



# The **Discrepancy** between Dynamical and Baryonic Surface Density of **Elliptical Galaxies**

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4th Jul. APRIM, Taipei

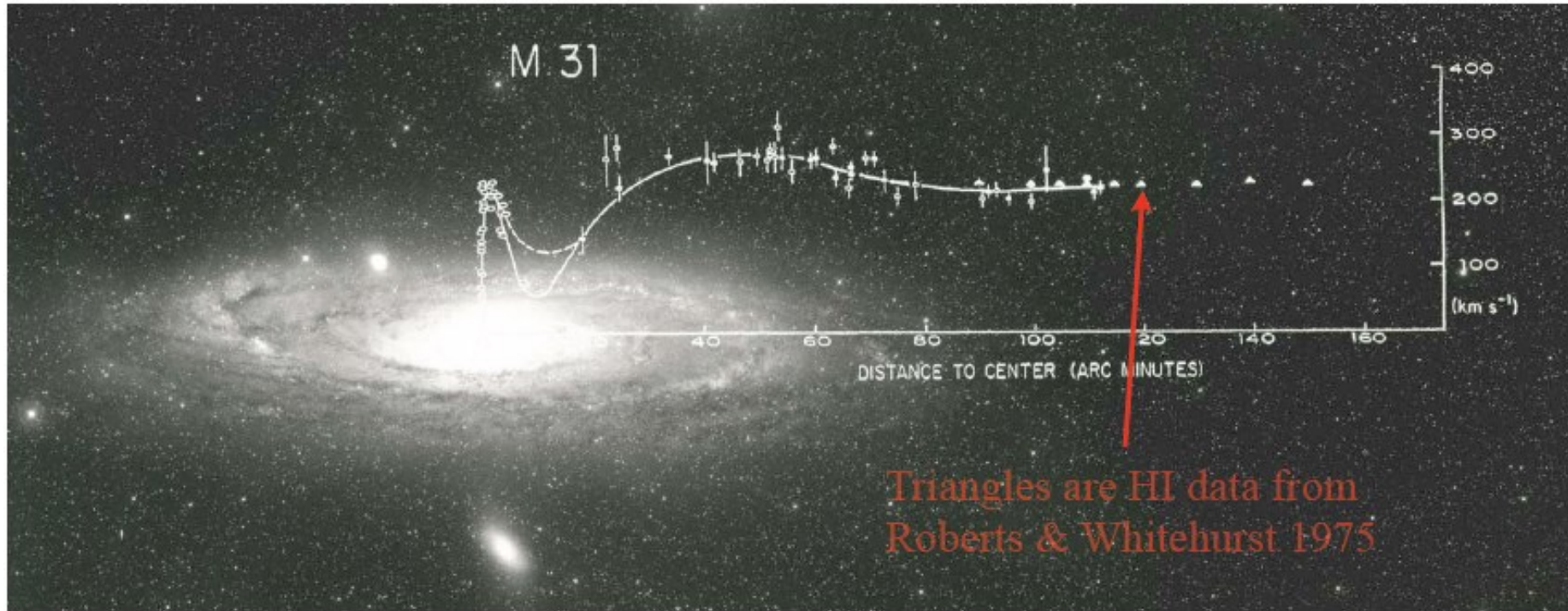


**2017 Asia-Pacific  
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3-7 July 2017, TAIPEI, TAIWAN

# Outline

- **The “Missing Mass” Problem**
- **Mass Acceleration-Discrepancy Relation**
- **Surface Density Discrepancy**
  - **Spiral Galaxies**
  - **Elliptical Galaxies**
- **Summary**

# Flat Rational Curves



1970 ApJ 159, 379

ROTATION OF THE ANDROMEDA NEBULA FROM A SPECTROSCOPIC  
SURVEY OF EMISSION REGIONS\*

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Department of Terrestrial Magnetism, Carnegie Institution of Washington and  
Lowell Observatory, and Kitt Peak National Observatory‡

$$\frac{v^2}{r} = \frac{GM}{r^2} \Rightarrow v \propto \frac{1}{\sqrt{r}}$$

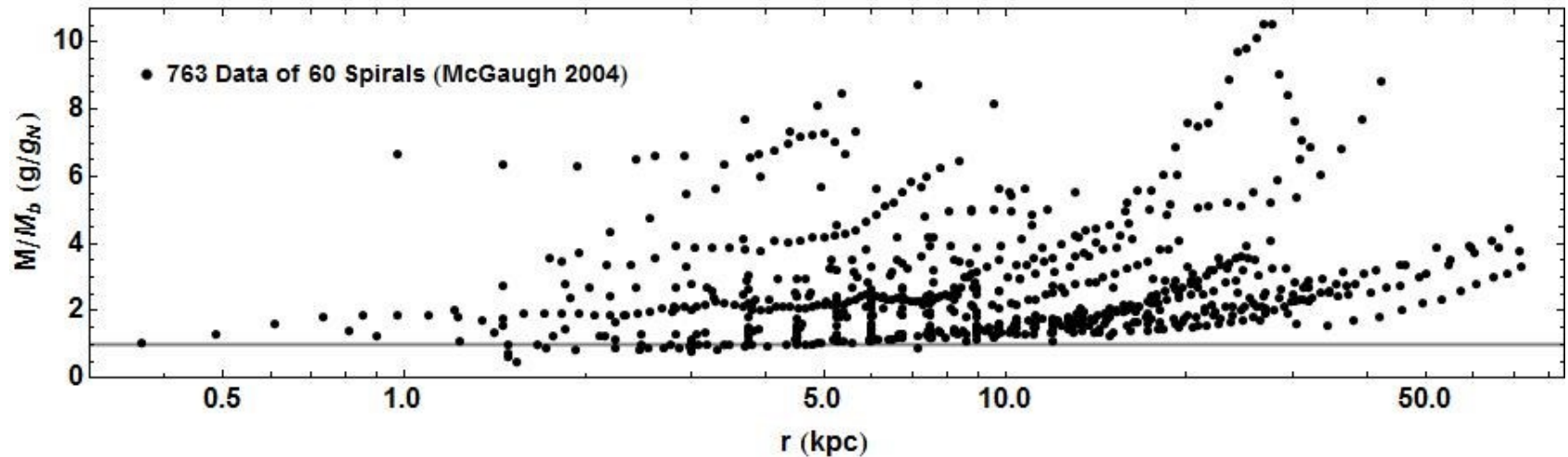
# THE MASS DISCREPANCY–ACCELERATION RELATION: DISK MASS AND THE DARK MATTER DISTRIBUTION

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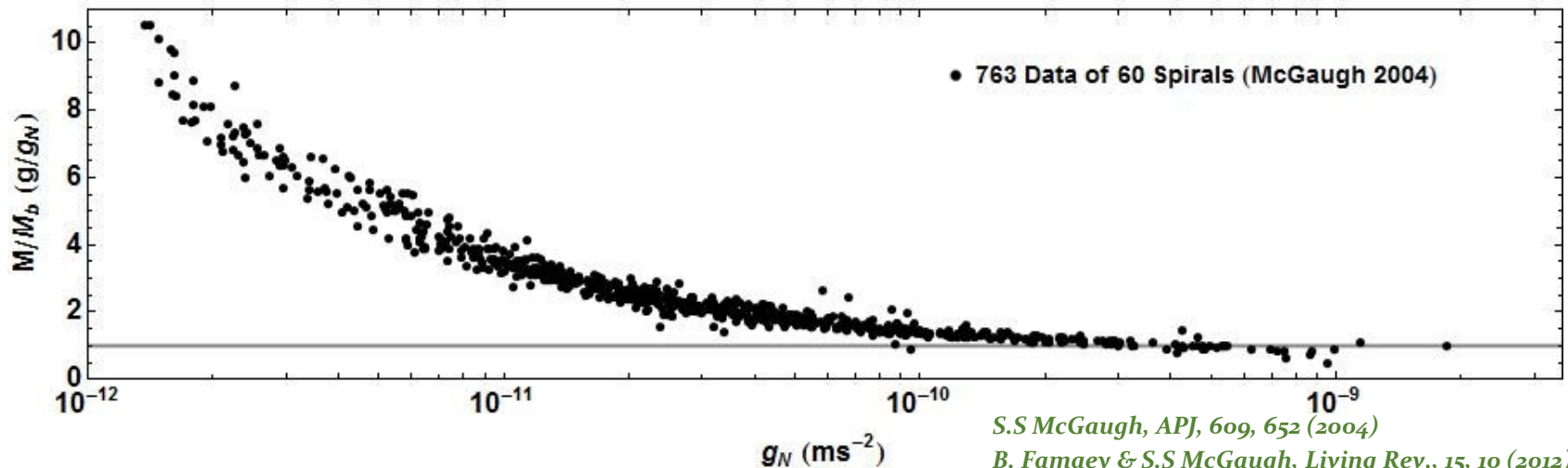
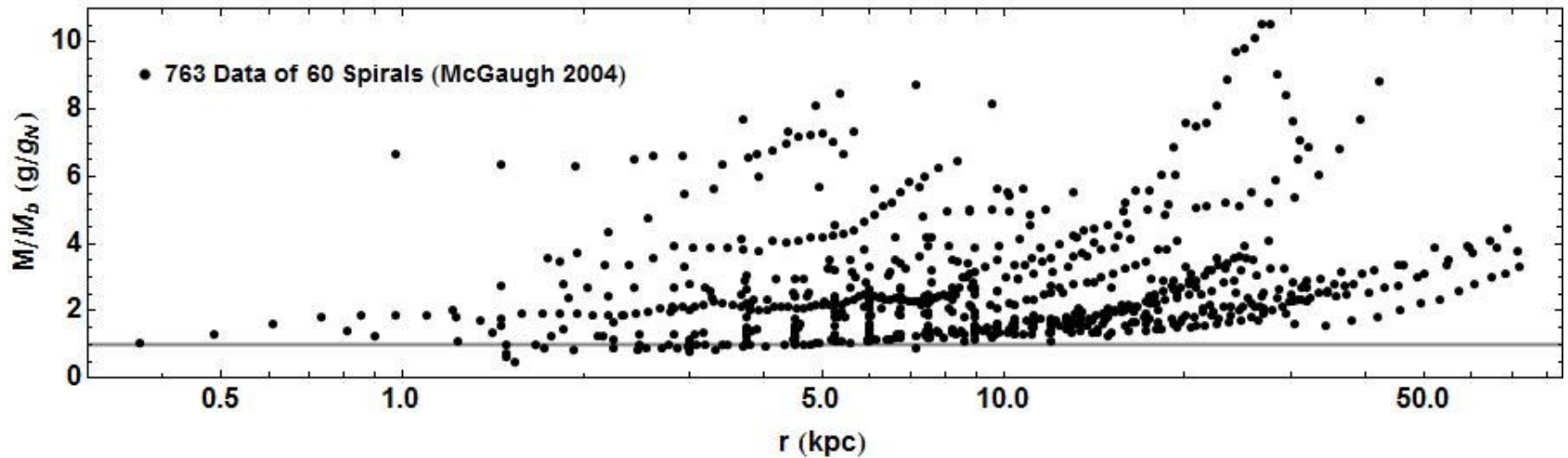
*Received 2003 July 12; accepted 2004 March 25*

$$g(r) = \frac{GM(r)}{r^2} = \frac{V^2}{r} \qquad \frac{g(r)}{g_N(r)} = \frac{M(r)}{M_b(r)} = \frac{V^2}{V_b^2}$$



# Mass Discrepancy-Acceleration Relation

$$g(r) = \frac{GM(r)}{r^2} = \frac{V^2}{r} \quad \frac{g(r)}{g_N(r)} = \frac{M(r)}{M_b(r)} = \frac{V^2}{V_b^2}$$



*S.S. McGaugh, APJ, 609, 652 (2004)*

*B. Famaey & S.S. McGaugh, Living Rev., 15, 10 (2012)*





## THE RELATION BETWEEN STELLAR AND DYNAMICAL SURFACE DENSITIES IN THE CENTRAL REGIONS OF DISK GALAXIES

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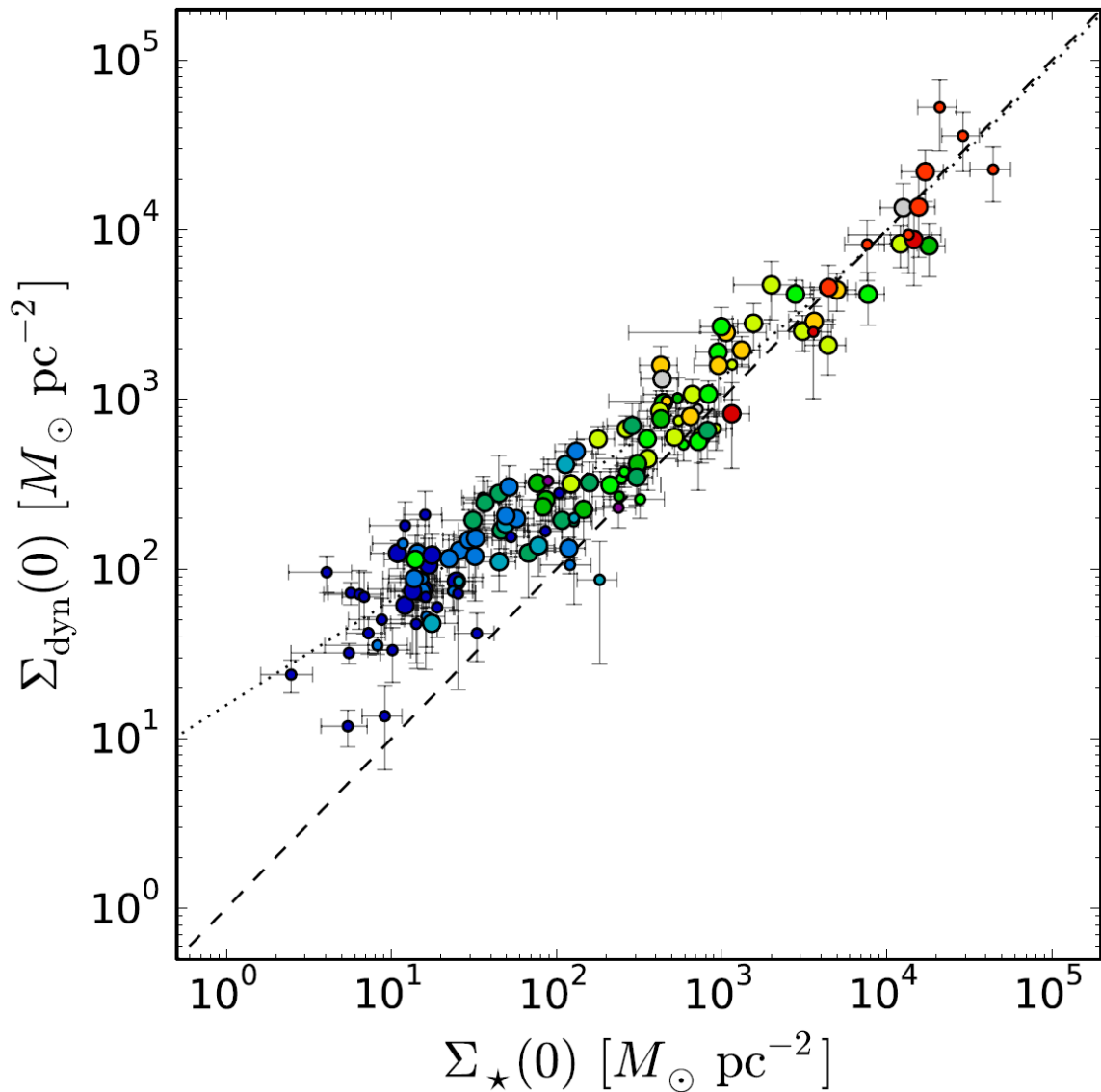
*Received 2016 June 9; revised 2016 July 4; accepted 2016 July 5; published 2016 August 10*

- **135** galaxies from SPARC database with **high-quality HI rotation curves** and **Spitzer surface photometry**.
- **Dynamical surface density** can be calculated from HI rotation curves by

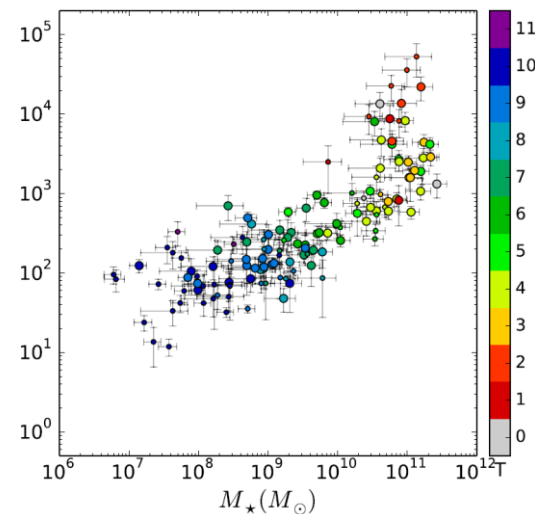
$$\Sigma_{\text{dyn}}(0) = \frac{1}{2\pi G} \int_0^{\infty} \frac{V^2(R)}{R^2} dR,$$

- **Stellar surface density** can be estimated from the near-IR surface brightness.

# Mass Discrepancy in Surface Density



$$\Sigma = \frac{M}{\pi r^2} \approx \frac{a}{G}$$



$$\Sigma_{\text{dyn}}(0) = \Sigma_0 \left[ 1 + \frac{\Sigma_\star(0)}{\Sigma_{\text{crit}}} \right]^{\alpha-\beta} \left[ \frac{\Sigma_\star(0)}{\Sigma_{\text{crit}}} \right]^\beta$$

$$\alpha = 0.97 \pm 0.06$$

$$\beta = 0.61 \pm 0.04$$

$$\Sigma_0 = \Sigma_{\text{crit}} = 1271 \pm 463 \quad [M_\odot \text{pc}^{-2}].$$



# Radial Acceleration Relation in Rotationally Supported Galaxies

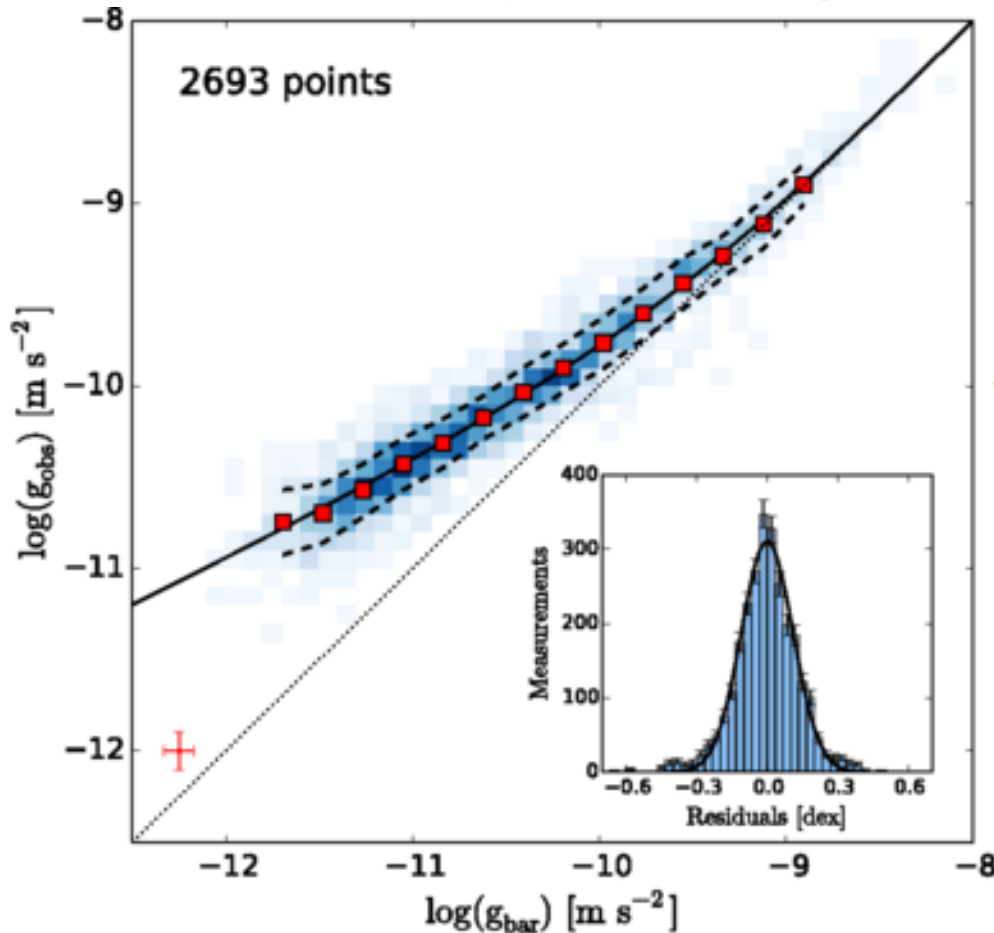
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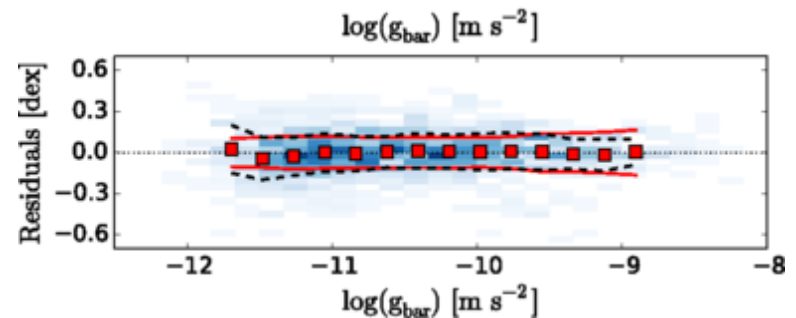
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(Received 18 May 2016; revised manuscript received 7 July 2016; published 9 November 2016)



$$g_{\text{DM}} = g_{\text{obs}} - g_{\text{bar}} = \frac{g_{\text{bar}}}{e^{\sqrt{g_{\text{bar}}/g_{\ddagger}} - 1}}$$

$$g_{\ddagger} = 1.20 \pm 0.02 \text{ (random)} \pm 0.24 \text{ (syst)} \times 10^{-10} \text{ ms}^{-2}$$





**Elliptical Galaxies?**

# An extensive catalogue of early-type galaxies in the nearby Universe

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*Departamento de Astronomía, Universidad de Concepcion, Casilla 160-C, Concepcion, Chile*

## ABSTRACT

We present a catalogue of 1715 early-type galaxies from the literature, spanning the luminosity range from faint dwarf spheroidal galaxies to giant elliptical galaxies. The aim of this catalogue

**Table 11.** Structural properties and internal dynamics of the galaxies in this catalogue. A portion of the table is shown here for guidance regarding its contents and form. A detailed description of the contents of this table is given in Section 7.2. The table in its entirety can be downloaded at <http://www.astro-udec.cl/mf/catalogue/>.

id	$R_e$ (pc)	$dR_e$ (pc)	s.	$n$	$dn$	s.	$\sigma_e$ (km s <sup>-1</sup> )	$+d\sigma_e$ (km s <sup>-1</sup> )	$-d\sigma_e$ (km s <sup>-1</sup> )	s.	$\sigma_0$ (km s <sup>-1</sup> )	$+d\sigma_0$ (km s <sup>-1</sup> )	$-d\sigma_0$ (km s <sup>-1</sup> )	s.	$v_{rot}$ (km s <sup>-1</sup> )	$+dv_{rot}$ (km s <sup>-1</sup> )	$-dv_{rot}$ (km s <sup>-1</sup> )	s.	$M_{dyn}$ [lg( $M_\odot$ )]	$dM_{dyn}$ [lg( $M_\odot$ )]	s.
501	1879.9	188.0	1	2.8	0.4	1	75.7	3.8	3.8	1	76.7	3.8	3.8	1	58.3	-9.9	-9.9	1	9.75	0.09	1
502	2433.1	243.3	1	4.2	1.7	1	82.0	4.1	4.1	1	91.8	4.6	4.6	1	21.9	-9.9	-9.9	1	9.70	0.09	1
503	2043.4	204.3	1	8.4	2.0	1	128.5	6.4	6.4	1	132.4	6.6	6.6	1	36.2	-9.9	-9.9	1	10.23	0.09	1
504	6949.9	-9.9	2	5.2	2.2	0	267.3	-9.9	-9.9	101	290.4	-9.9	-9.9	2	-9.9	-9.9	-9.9	0	11.68	-99.99	101
505	2393.8	239.4	1	4.4	0.4	1	62.2	3.1	3.1	1	56.2	2.8	2.8	1	8.5	-9.9	-9.9	1	9.65	0.09	1

**Table 15.** Stellar populations of the galaxies in this catalogue. A portion of the table is shown here for guidance regarding its contents and form. A detailed description of the contents of this table is given in Section 8.2. The table in its entirety can be downloaded at <http://www.astro-udec.cl/mf/catalogue/>.

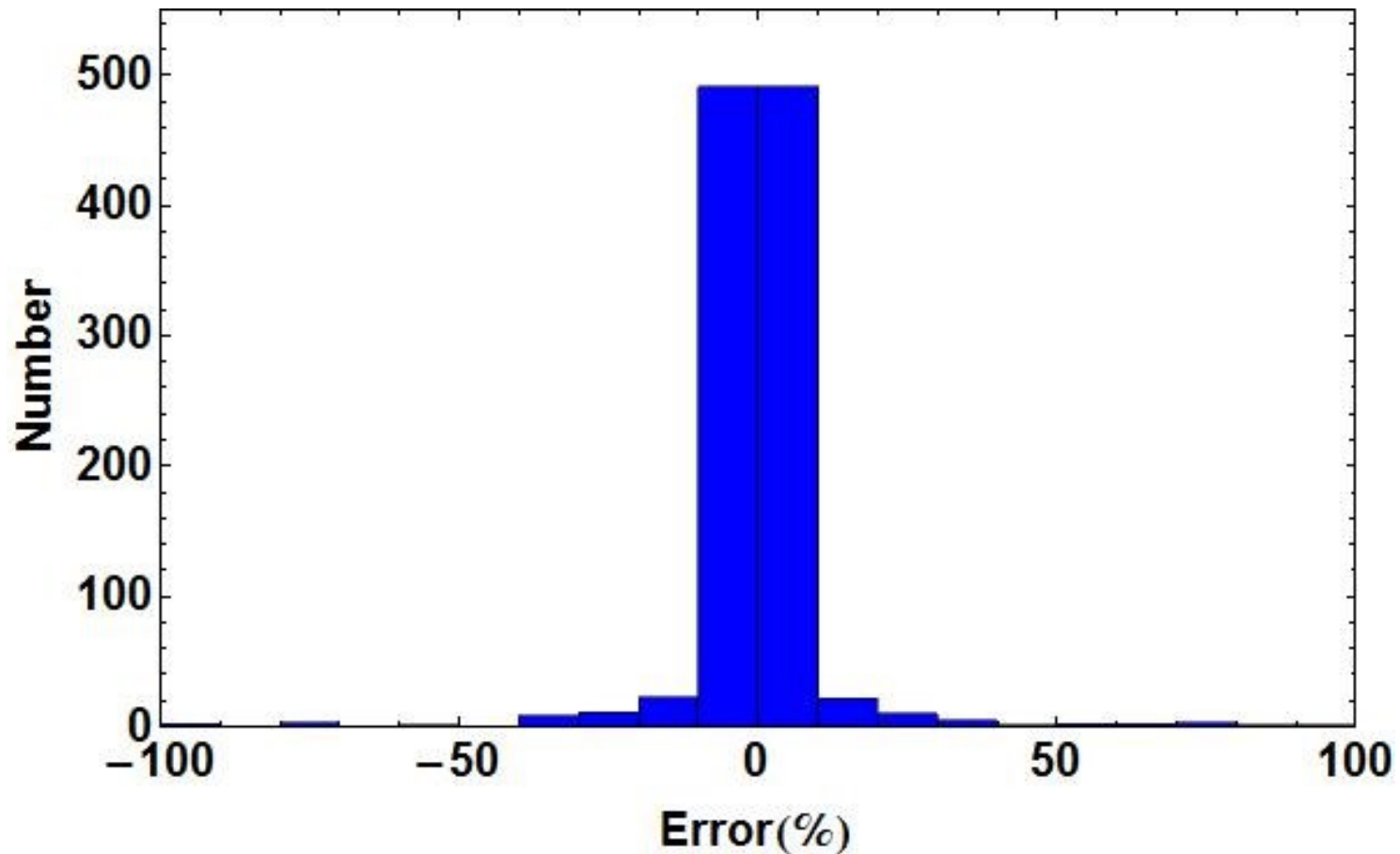
id	$t$ (Gyr)	$+dt$ (Gyr)	$-dt$ (Gyr)	s.	[Z/H]	$+d[Z/H]$	$-d[Z/H]$	s.	$M_s$ lg( $M_\odot$ )	$dM_s$ lg( $M_\odot$ )	s.
501	3.5	0.6	0.6	1	-0.38	0.06	0.06	1	9.81	-99.99	1011
502	1.0	0.1	0.1	1	0.18	0.06	0.06	1	9.68	-99.99	1011
503	9.7	1.6	1.6	1	-0.36	0.05	0.05	1	10.09	-99.99	1011
504	-9.9	-9.9	-9.9	0	0.06	99.99	99.99	1020	11.46	-99.99	1020
505	2.5	0.3	0.3	1	-0.78	0.06	0.06	1	9.18	-99.99	1011

# An extensive catalogue of early-type galaxies in the nearby Universe

J. Dabringhausen<sup>★</sup> and M. Fellhauer<sup>★</sup>

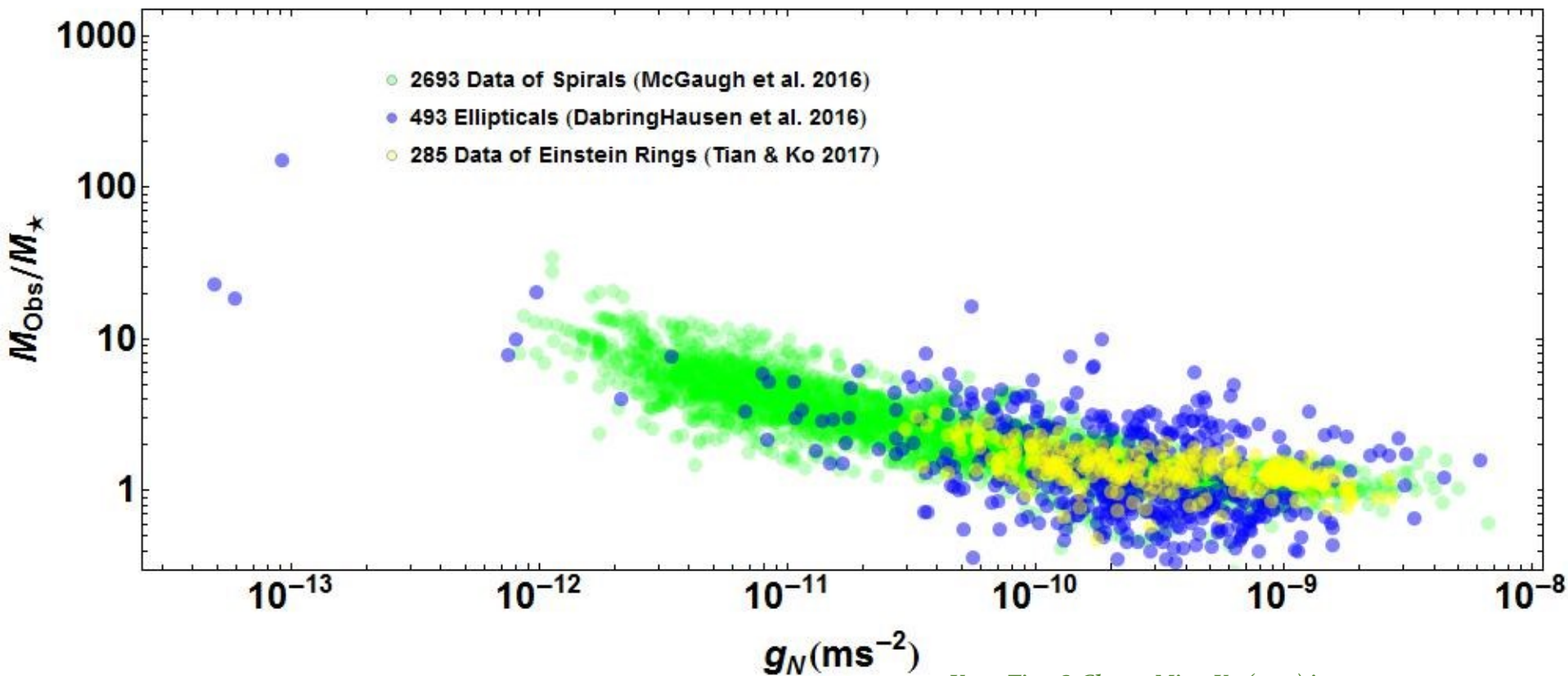
*Departamento de Astronomía, Universidad de Concepcion, Casilla 160-C, Concepcion, Chile*

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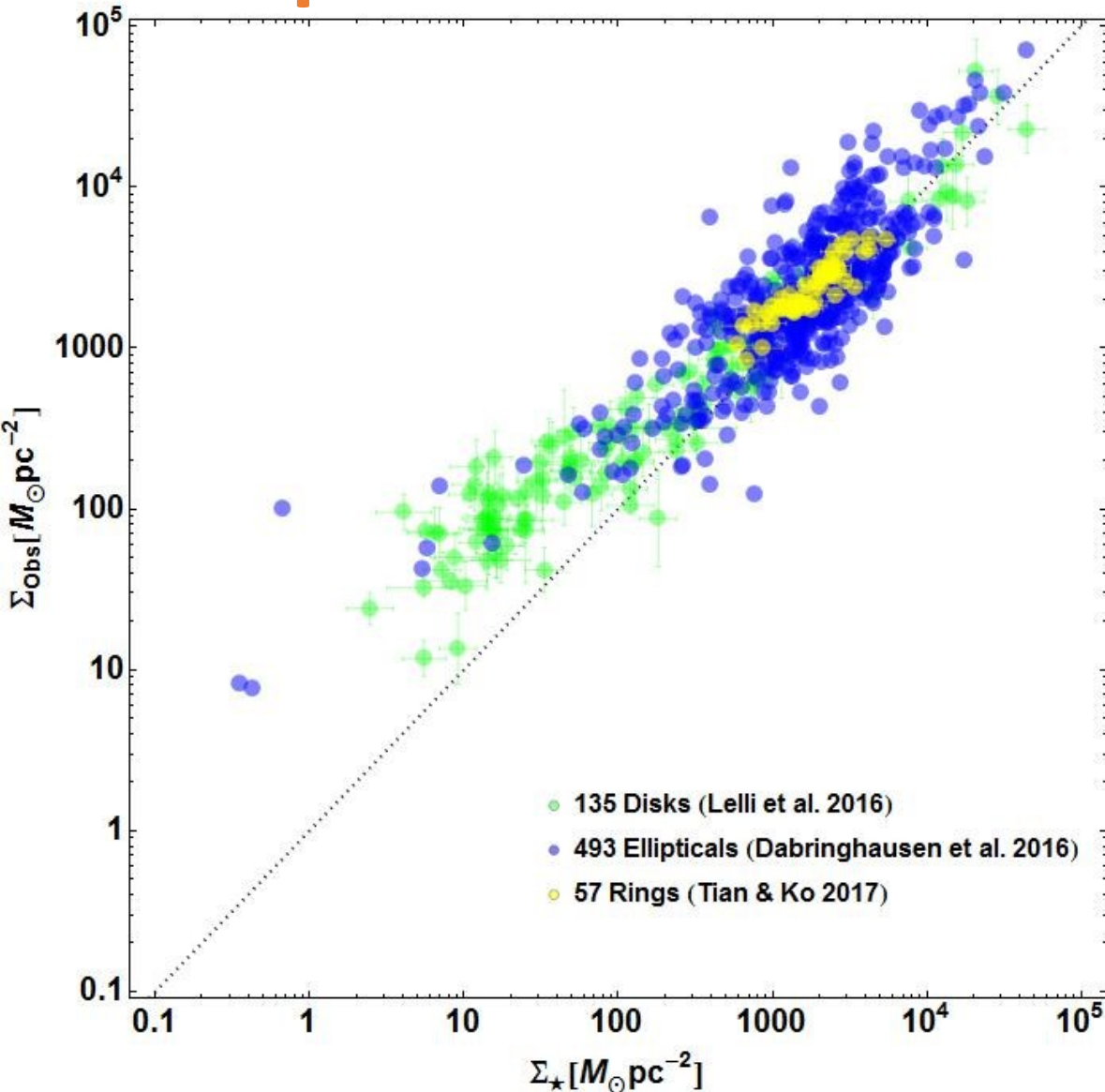


# Mass Discrepancy-Acceleration Relation in Elliptical Galaxies

$$g(r) = \frac{GM(r)}{r^2} \quad \frac{g(r)}{g_N(r)} = \frac{M(r)}{M_b(r)}$$



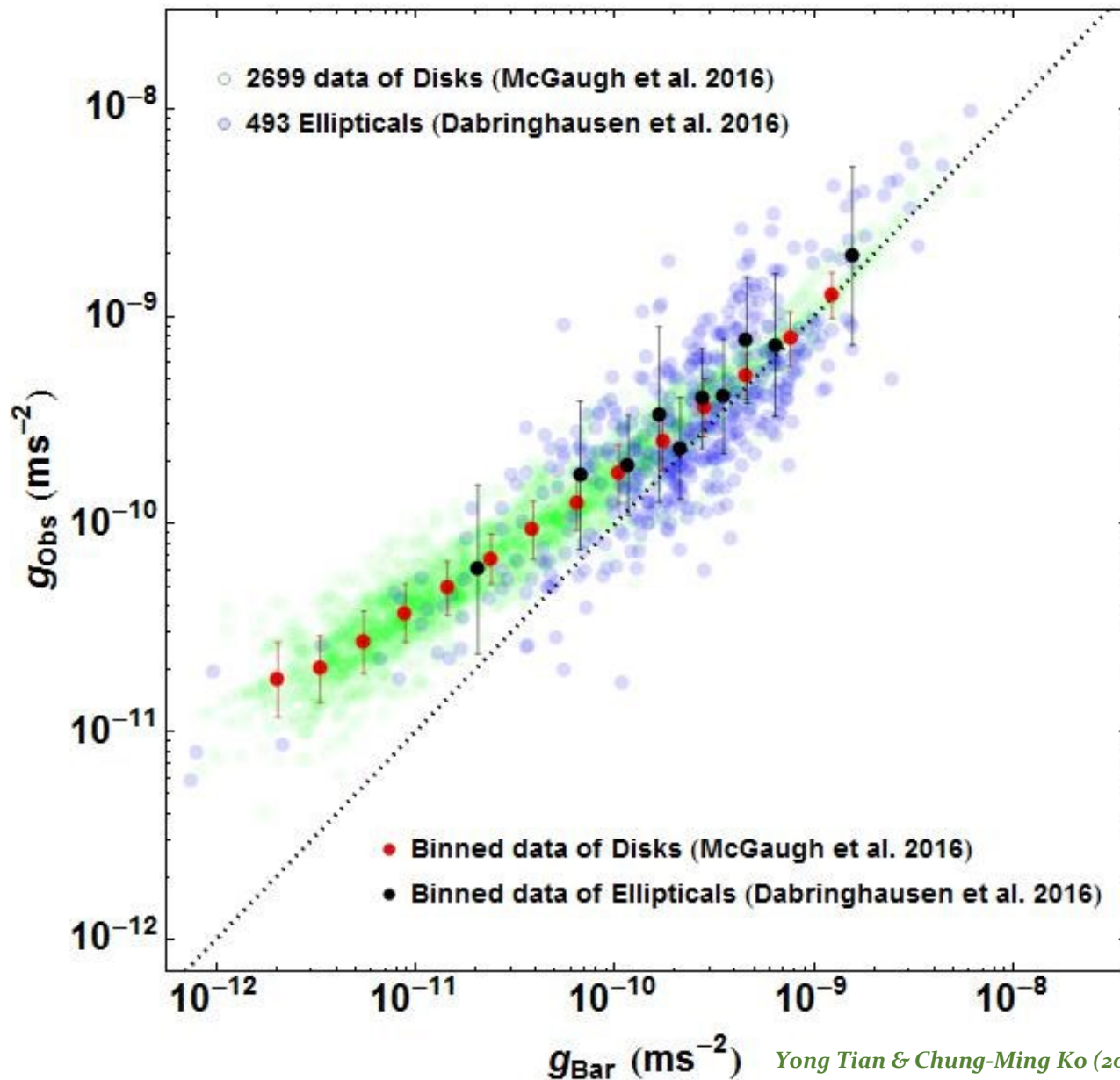
# Surface Density Discrepancy in Elliptical Galaxies



$$\Sigma = \frac{M}{\pi r^2} \approx \frac{a}{G}$$



# Radial Acceleration Relation



# Surface Density Discrepancy in Modified Newtonian Dynamics

## ➤ Modified Newtonian Dynamics (MOND)

$$g \approx g_N \nu(g_N/a_0) \quad \begin{array}{l} \nu(y \gg 1) \approx 1 \\ \nu(y \ll 1) \approx y^{-1/2} \end{array}$$
$$a_0 = 1.2 \times 10^{-10} m s^{-2}$$

## ➤ The surface density

$$\Sigma = \frac{M}{\pi r^2} \approx \frac{a}{G}$$

## ➤ In MOND, the criterion is

$$\Sigma_0 \equiv \frac{a_0}{G} = 276 M_\odot pc^{-2}$$

## ➤ High-Surface-Density galaxies are as $\Sigma > \Sigma_0$

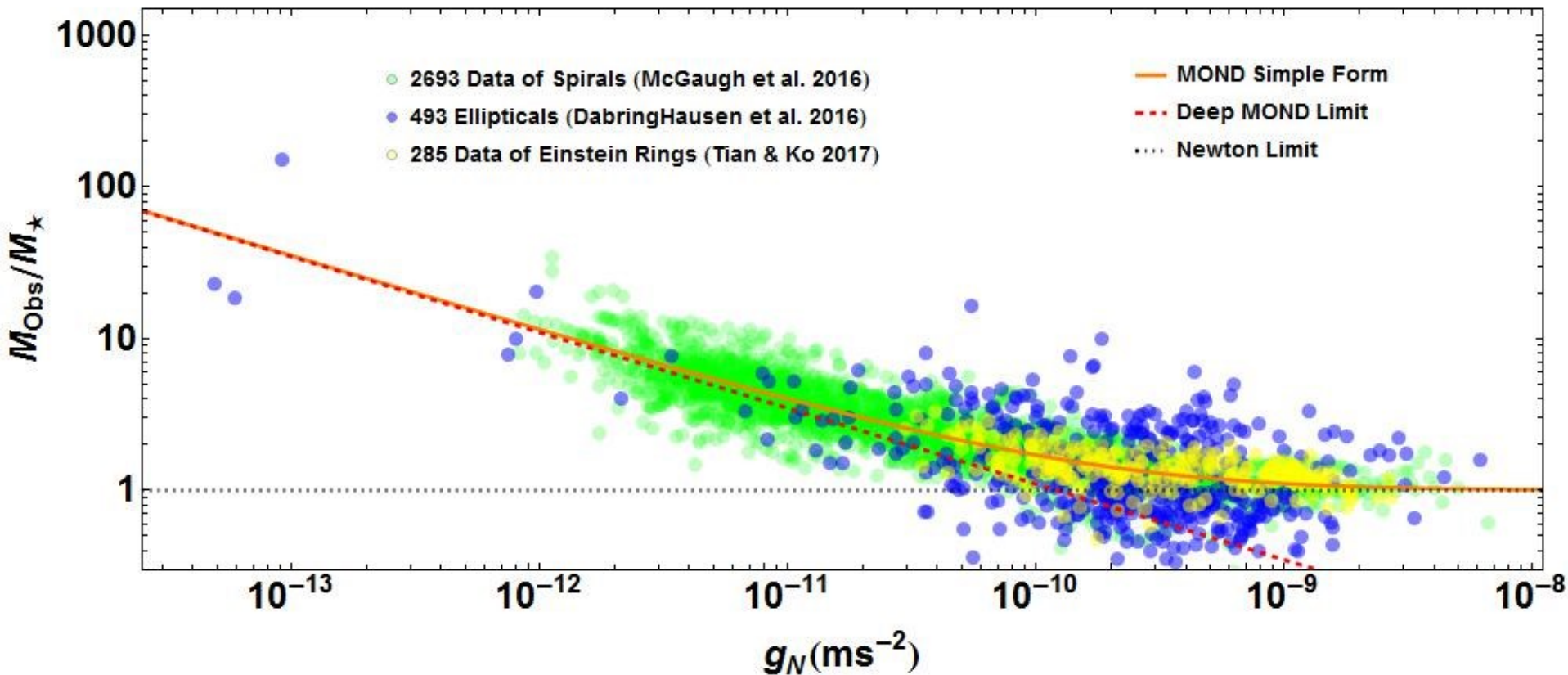
## ➤ Low-Surface-Density galaxies are as $\Sigma < \Sigma_0$

*Milgrom, ApJ (1983)*

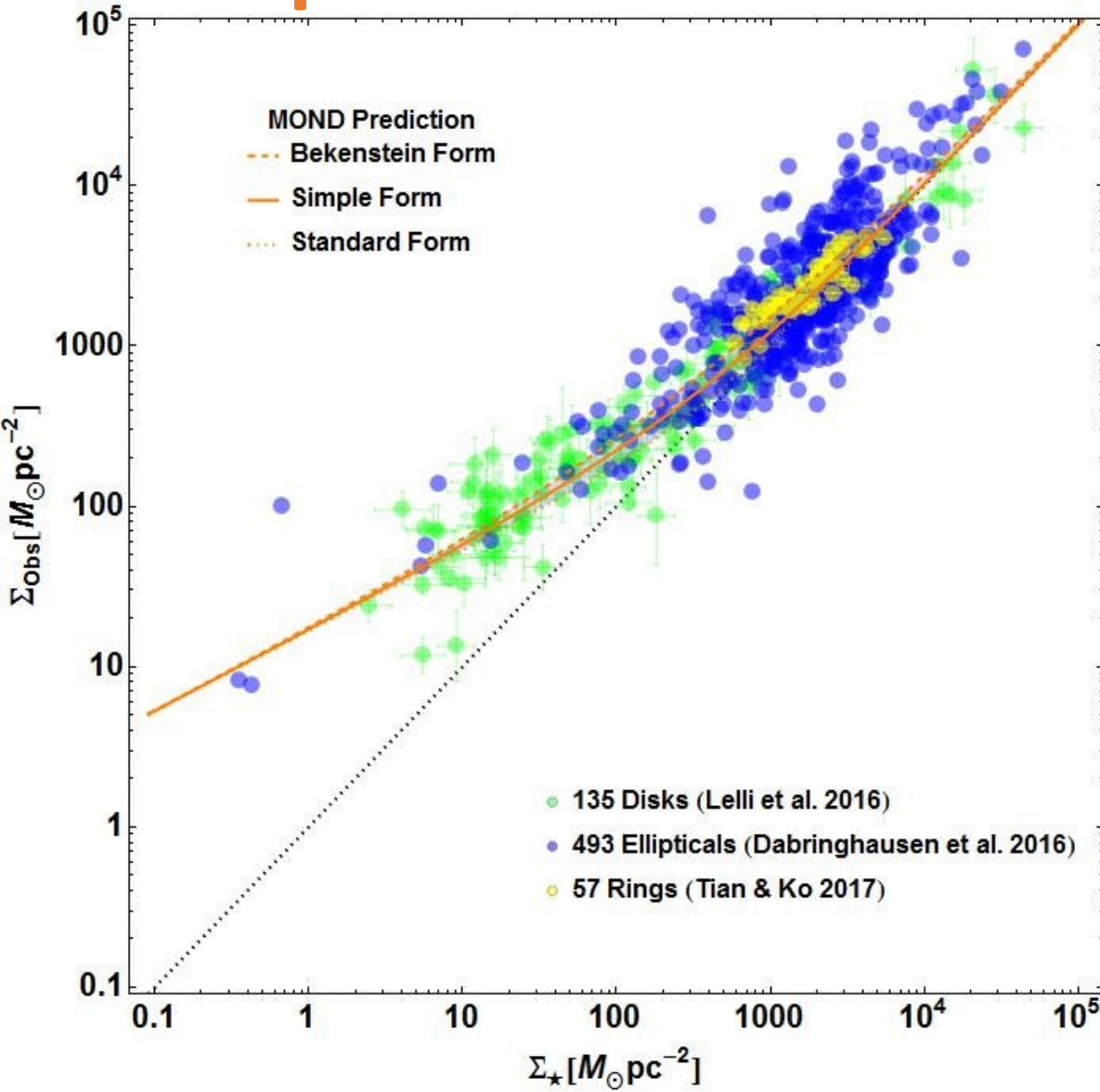
*Sanders & McGaugh, ARAA (2002)*

# Mass Discrepancy-Acceleration Relation in Elliptical Galaxies

$$g(r) = \frac{GM(r)}{r^2} \quad \frac{g(r)}{g_N(r)} = \frac{M(r)}{M_b(r)} = \nu(y)$$



# Surface Density Discrepancy in Elliptical Galaxies

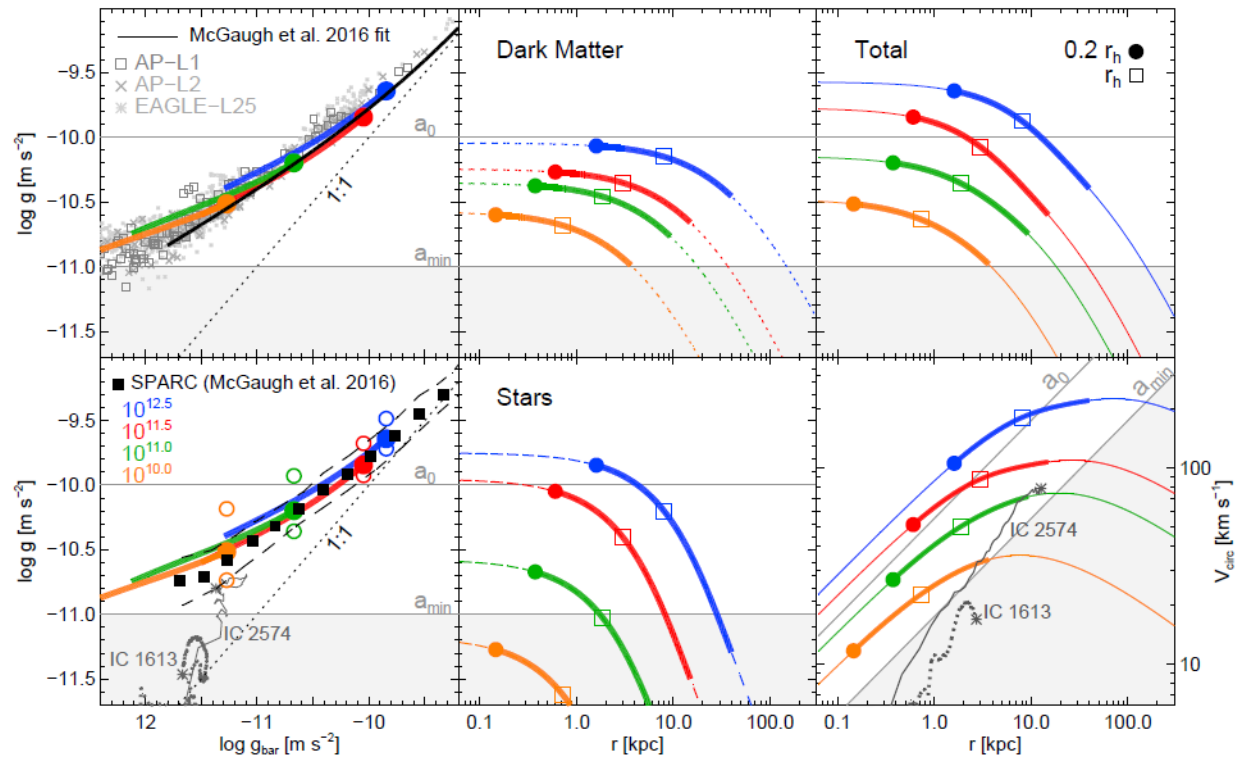


$$\Sigma = \frac{M}{\pi r^2} \approx \frac{a}{G}$$

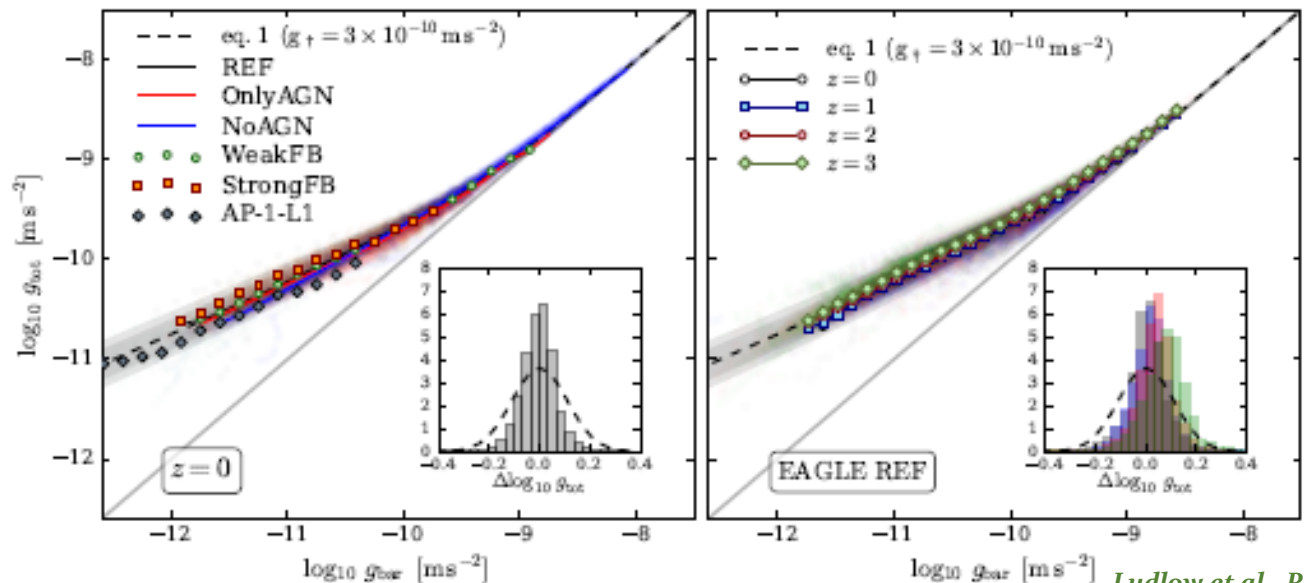
$$\Sigma_0 \equiv \frac{a_0}{G} = 276 M_{\odot} \text{pc}^{-2}$$

# $\Lambda$ CDM

- Semi-empirical models (Navarro et al. 2016)
- Hydro-dynamical simulations (Wu & Kroupa 2015; Ludlow et al. 2017)



Navarro et al. 2016 (arXiv:1612.06239)



Ludlow et al., PRL, 2017



# Summary

- **Mass Acceleration-Discrepancy Relation (MDAR)** and **Surface Density Discrepancy** in Elliptical galaxies is **consistency** with the result in the spiral galaxies.
- **MDAR** and **Surface Density Discrepancy** can be explained in MOND and  $\Lambda$ CDM.



## An extensive catalogue of early-type galaxies in the nearby Universe

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If  $\sigma_0$  and  $R_e$  are known for an ETG in this catalogue, its dynamical mass is calculated with

$$M_{\text{dyn}} = \frac{K_V}{G} R_e \sigma_0^2, \quad (13)$$

where  $K_V$  is a factor that depends on the shape of the density profile of the ETG and  $G$  is the gravitational constant. We approximate  $K_V$  with equation 11 in Bertin, Ciotti & Del Principe (2002), i.e.

$$K_V(n) = \frac{73.32}{10.465 + (n - 0.94)^2} + 0.954, \quad (14)$$

where  $n$  is the Sérsic index.

$$\log_{10} \left( \frac{\sigma_0}{\text{km s}^{-1}} \right) = 1.0478 \log_{10} \left( \frac{\sigma_e}{\text{km s}^{-1}} \right) - 0.0909 \quad (11)$$