

APRIM 2017, July 4th, 14:45-15:00, Room 201 A, 2F

Luminosities of ice giants with condensate in early atmosphere

Kurosaki & Ikoma (2017)

Kenji Kurosaki¹
Masahiro Ikoma²

1, Nagoya University

2, The University of Tokyo

Ice Giants



Ice giants in solar system
Uranus & Neptune

Both planets are in distant region

Uranus: 30,588 days

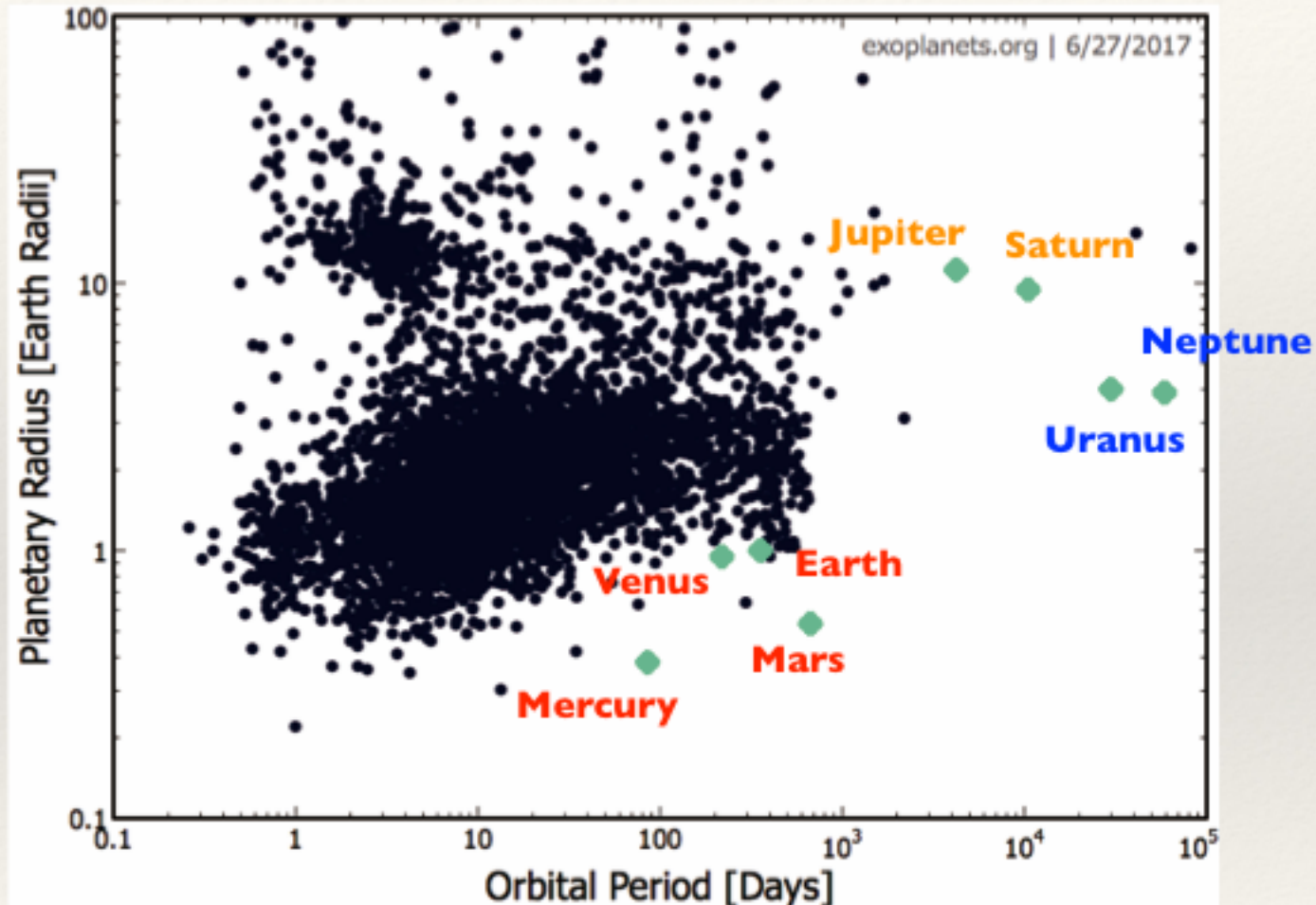
Neptune: 59,799 days

The atmosphere is enriched in heavy elements.

e.g.) Marley & McKay (1999) Fortney et al. (2011)

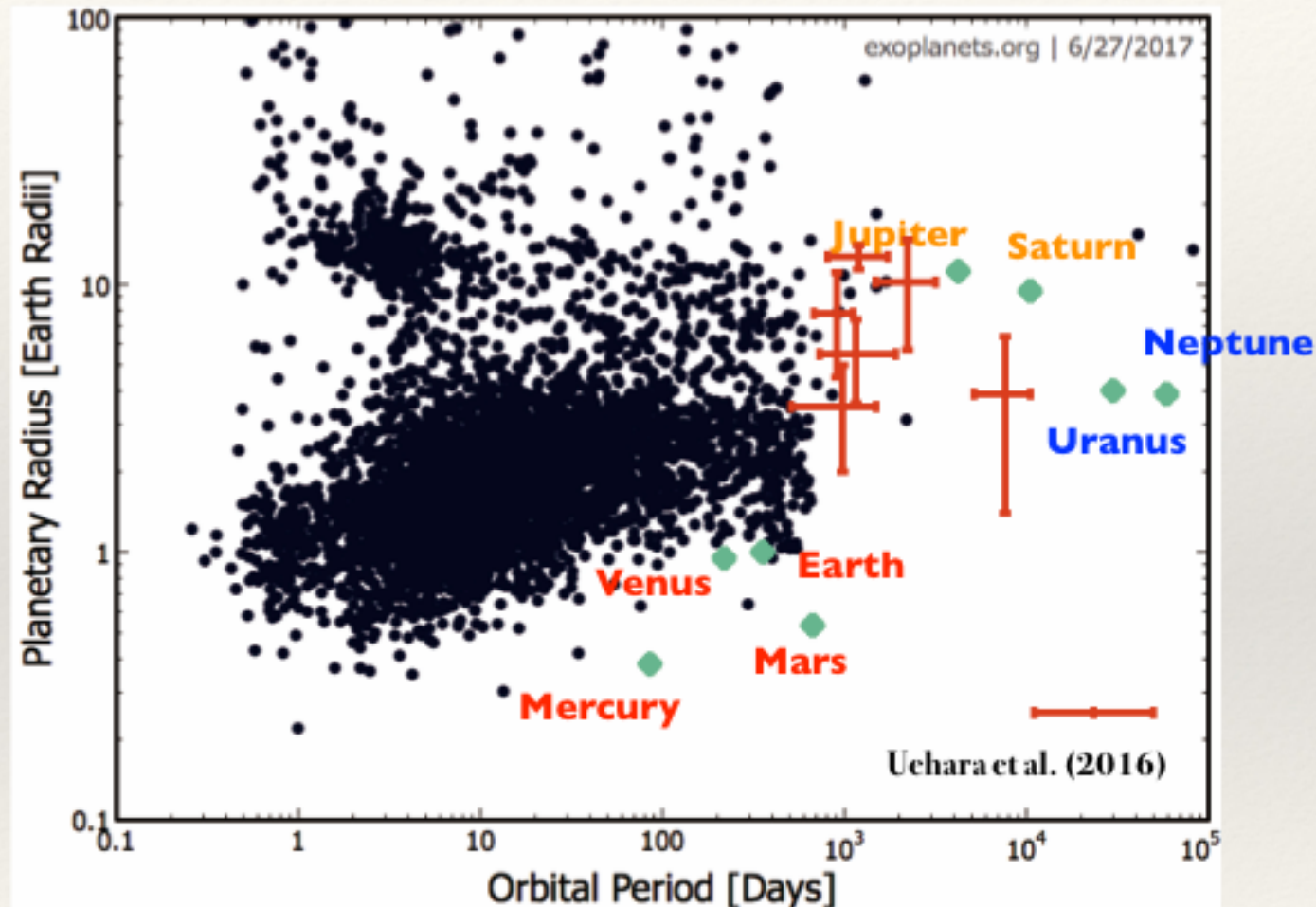
Extra-solar system: Many Neptune-size planets are detected.

Neptune-size Planets



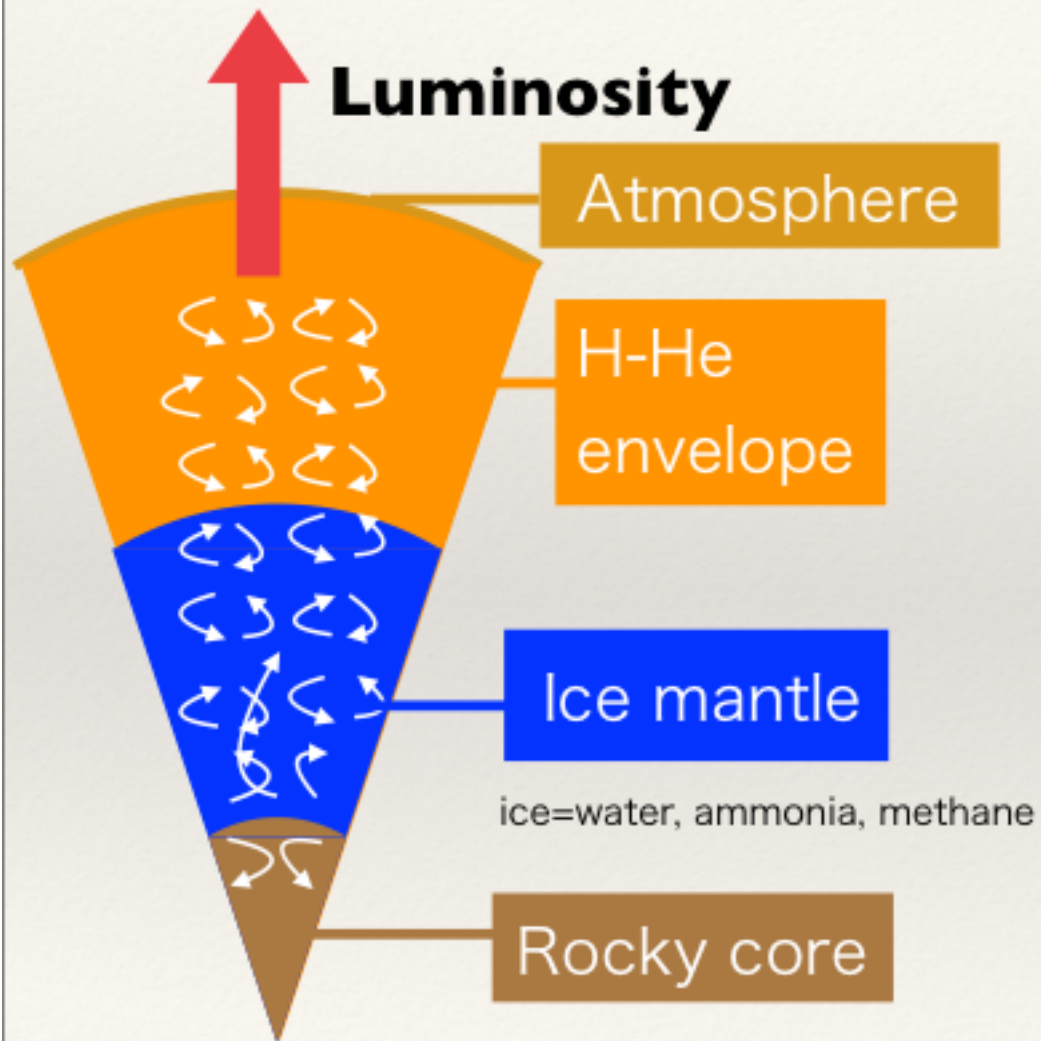
Most of all Neptune-size planets are in hot-region

Neptune-size Planets at Distant Region



Can we detect those distant planets by direct imaging?

How to estimate the Luminosity



The thermal evolution model constructed by Hubbard (1977)

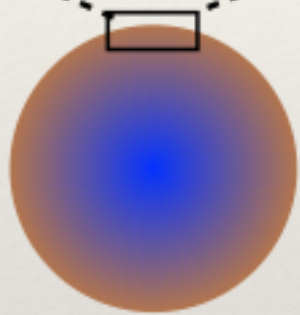
→ The model explains the present luminosity of Jupiter

Assumptions

1. Fully convective interior
2. The compositional distribution is unchanged through the evolution
3. Condensation is ignored
4. The planet possesses a high luminosity immediately after the formation

Atmosphere: Enriched in Heavy Elements

An atmosphere with a significant amount of ice



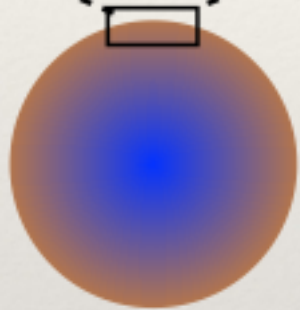
What will happen if the planet has an atmosphere enriched in icy materials

- Opacity will increase
- Heat capacity will become smaller
- Condensation will occur

**The planetary flux will be
Increased? Decreased?**

Atmosphere: Enriched in Heavy Elements

An atmosphere with a significant amount of ice



What will happen if the planet has an atmosphere enriched in icy materials

- Opacity will increase
- Heat capacity will become smaller
- Condensation will occur

**The planetary flux will be
Increased? Decreased?**

Latent heat due to the condensation heats up the atmosphere

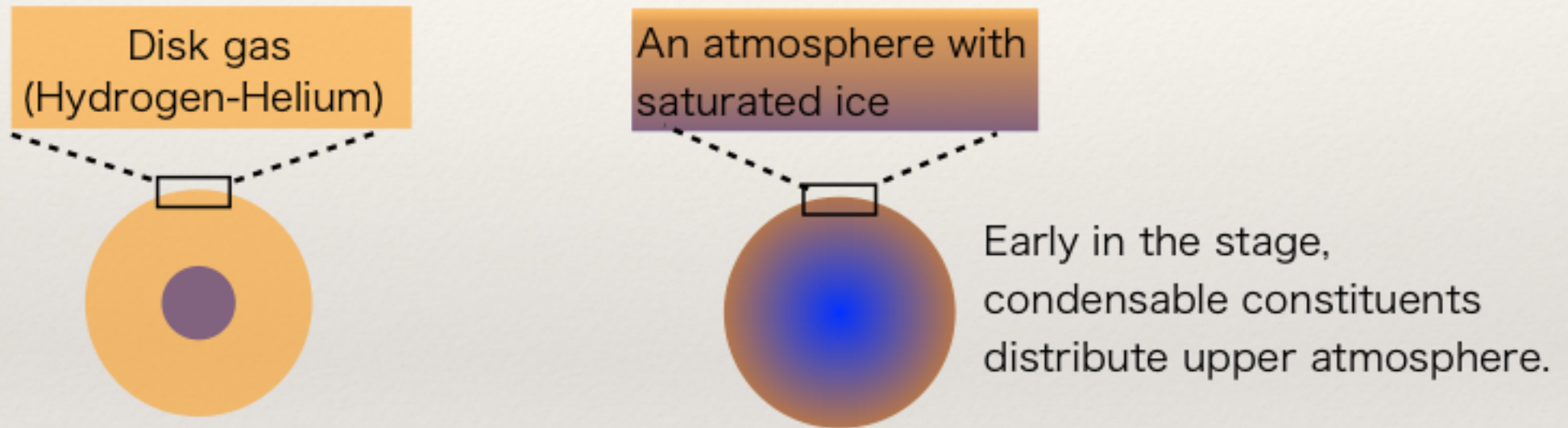
The planetary flux should be *increased*

Demonstrate the effect by solving the interior & atmosphere

Purpose of this Study

Purpose of this Study

We investigate the thermal evolution of the ice giant with a significant amount of ice constituents (water, ammonia, and methane) in the atmosphere

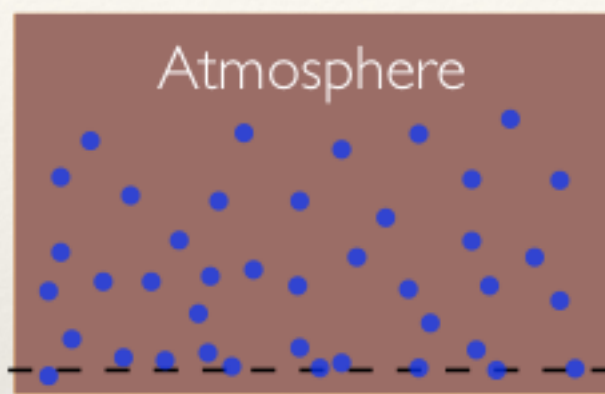


No studies focused on the thermal evolution of the ice giant with a significant amount of ice constituents in the atmosphere

We discuss the difference of the planetary luminosity with/without the effect of the condensation of water, ammonia, and methane.

Method: Model Summary

Methods: Model Summary



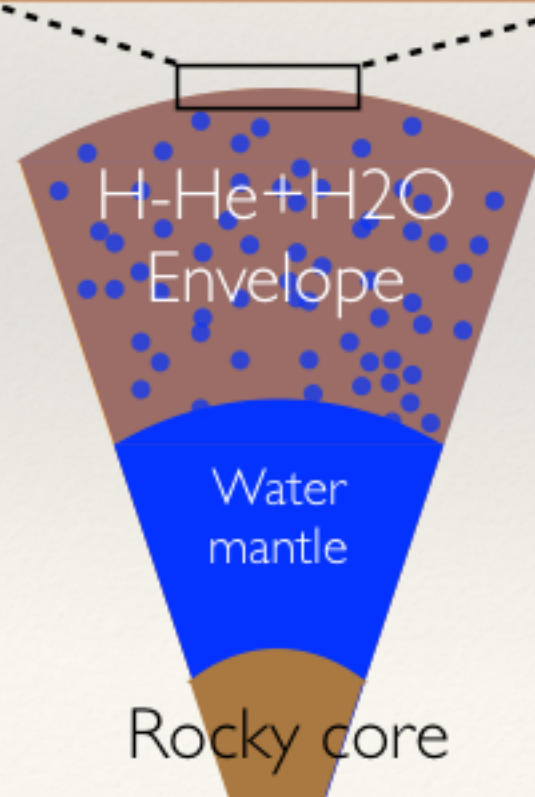
Atmosphere

Radiative-convective equilibrium

Constituents: H₂, He, H₂O, NH₃, CH₄

Condensates: H₂O, NH₃, CH₄

Boundary between the interior and atmosphere=100 bar



Envelope → Hydrogen, Helium, Water

Mantle → Water

Core → Rock (MgSiO₃)

Convective equilibrium (Isentropic)

Parameters:

Initial ice mole fraction in the atmosphere

NH₃/H₂O=0.135 (solar value of N/O)

CH₄/H₂O=0.056 (smaller than solar value of C/O)

Methods: Thermal Evolution

Fully convective interior \longrightarrow Constant entropy in each layer

$$\frac{\partial L_r}{\partial M_r} = -T \frac{dS}{dt} \Rightarrow \text{integrate by mass} \quad \int_0^{M_p} \frac{\partial L_r}{\partial M_r} dM_r = L_p = 4\pi R_p^2 F_p$$

The thermal evolution timescale is calculated by this equation

$$4\pi R_p^2 F_{\text{top}} = - \left[\frac{dS_{\text{env}}}{dt} \int_{M_c}^{M_p} T dM_r + \frac{dS_c}{dt} \int_0^{M_c} T dM_r \right]$$

Atmospheric structure

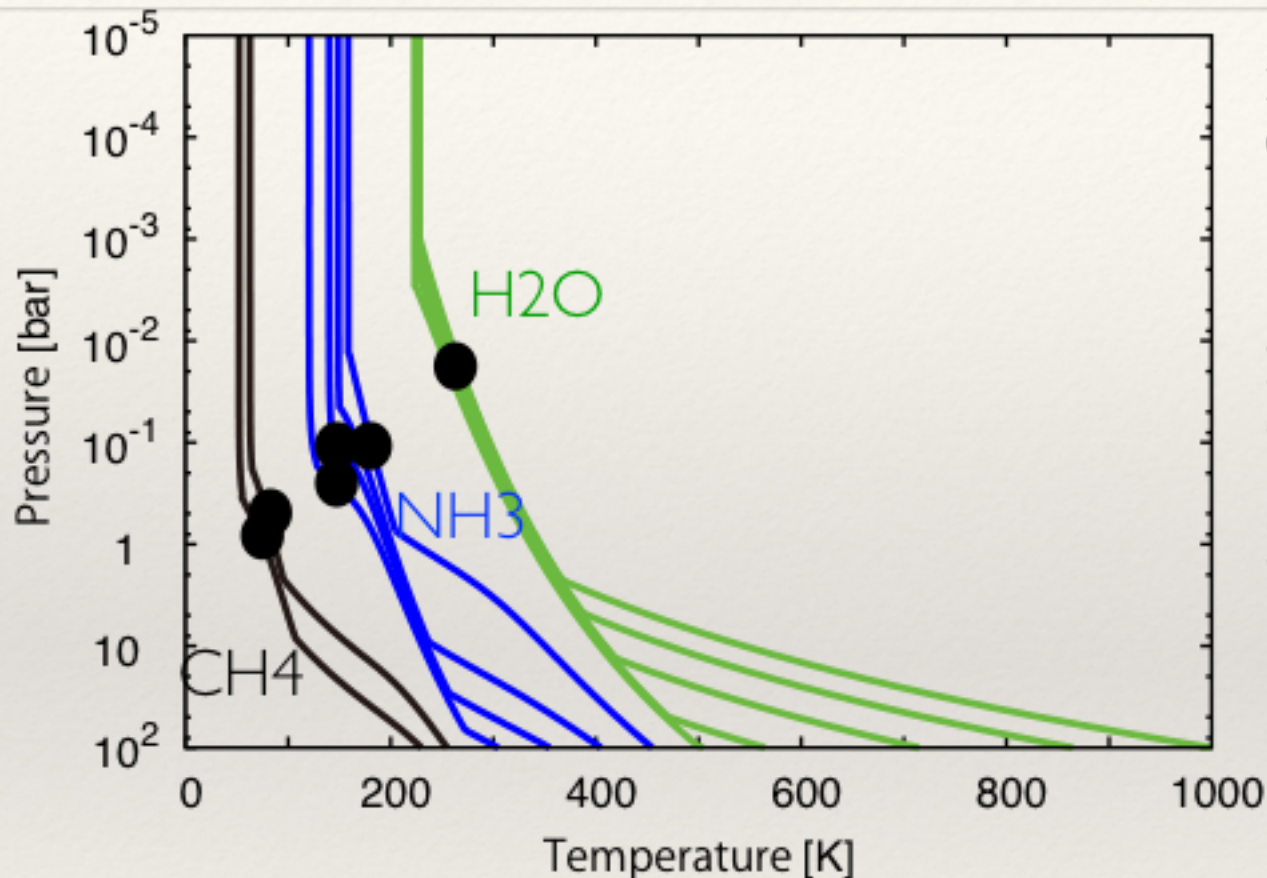
Cooling efficiency

Interior structure

Heat capacity

Calculate the atmospheric structure and interior structure simultaneously.

Atmospheric Structure Enriched in Ices



Ice constituents:
65 mol % in the atmosphere

● Optical depth = 1

NH₃/H₂O=0.135

CH₄/H₂O=0.056

Equilibrium temperature = 58.2K

← Time evolution

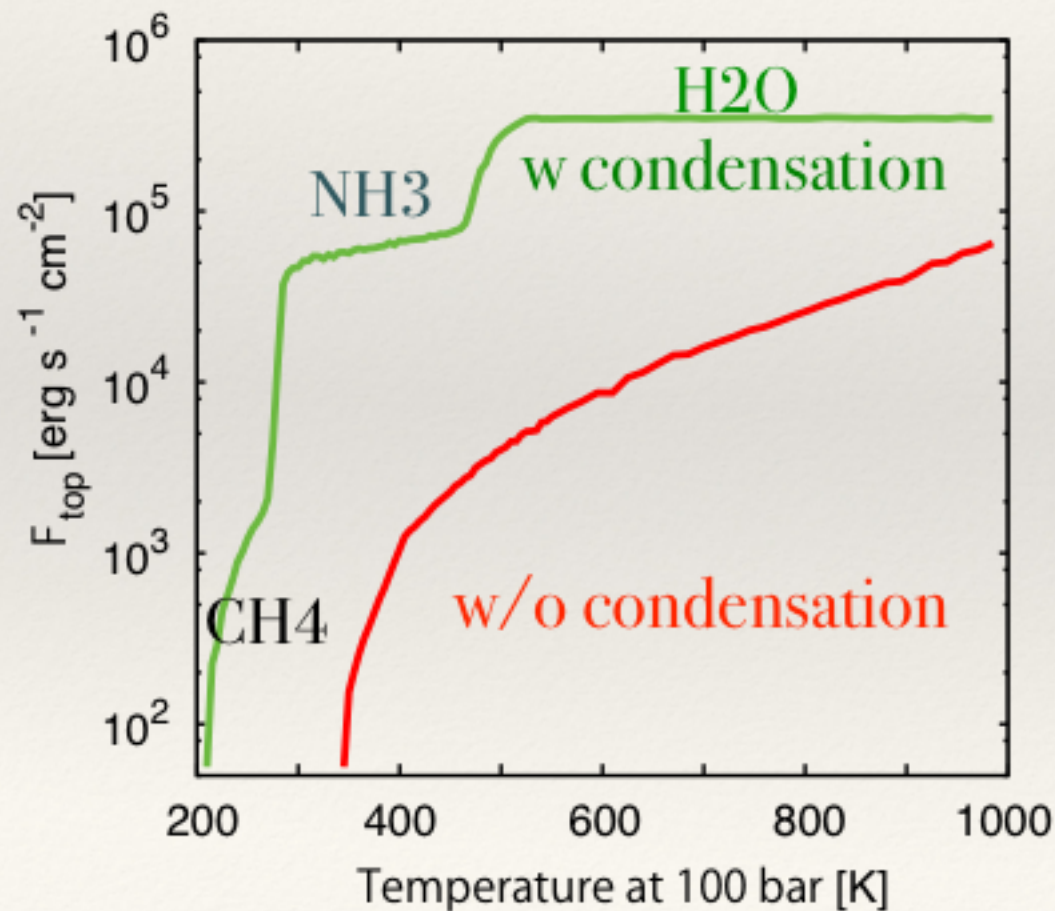
As the time passes, the bottom temperature decreases.

→ The main condensate changes as the time passes.

The Outgoing Flux from the Atmosphere

Ice constituents: 65 mol % in the atmosphere

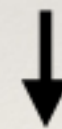
F_{top} : the outgoing flux from the top of the atmosphere



Main Condensate



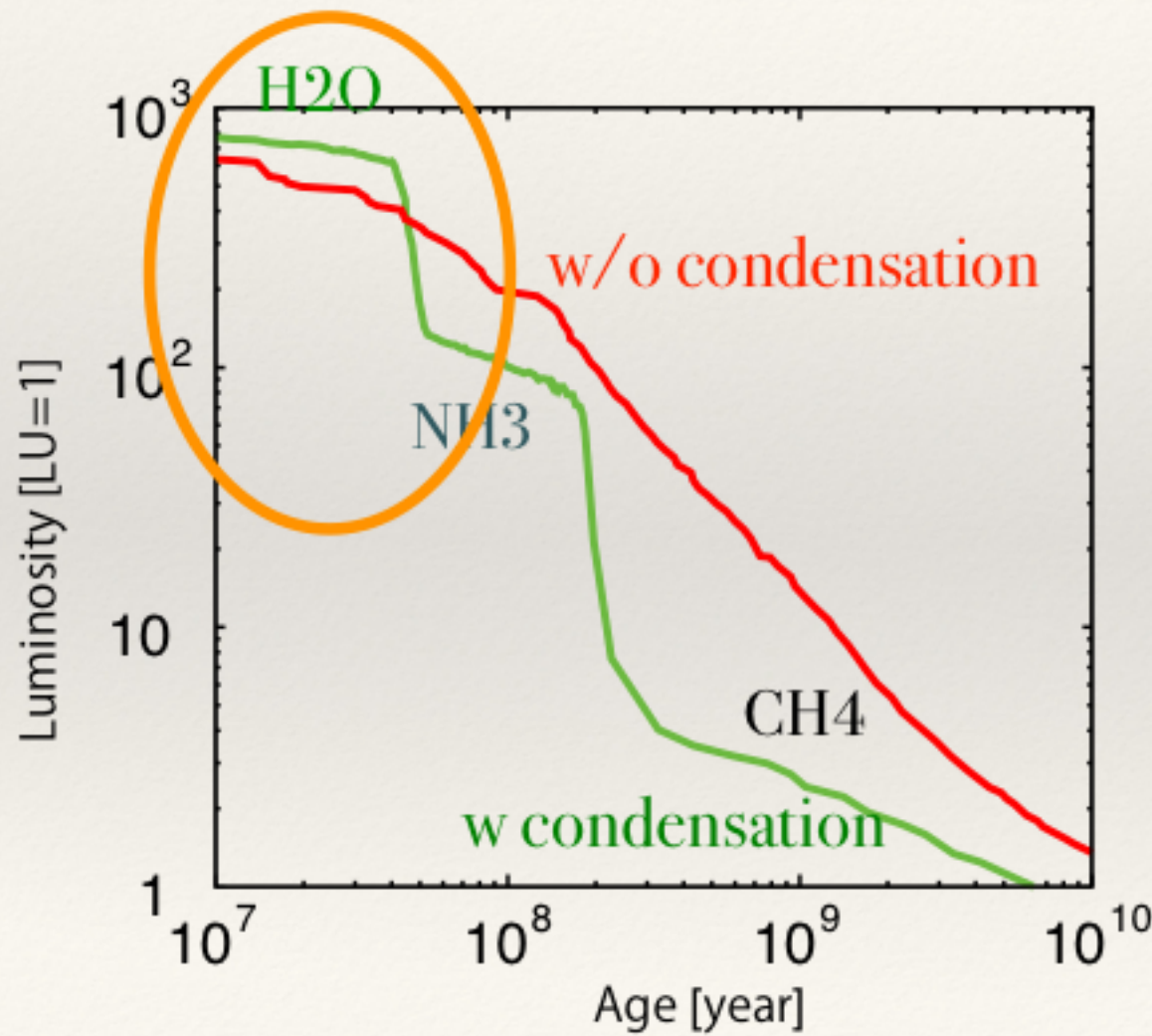
The temperature structure is changed by the condensation



Increase the planetary flux

The Effect on the Luminosity at Early Stage

Ice constituents: 65 mol % in the atmosphere



Increase the flux



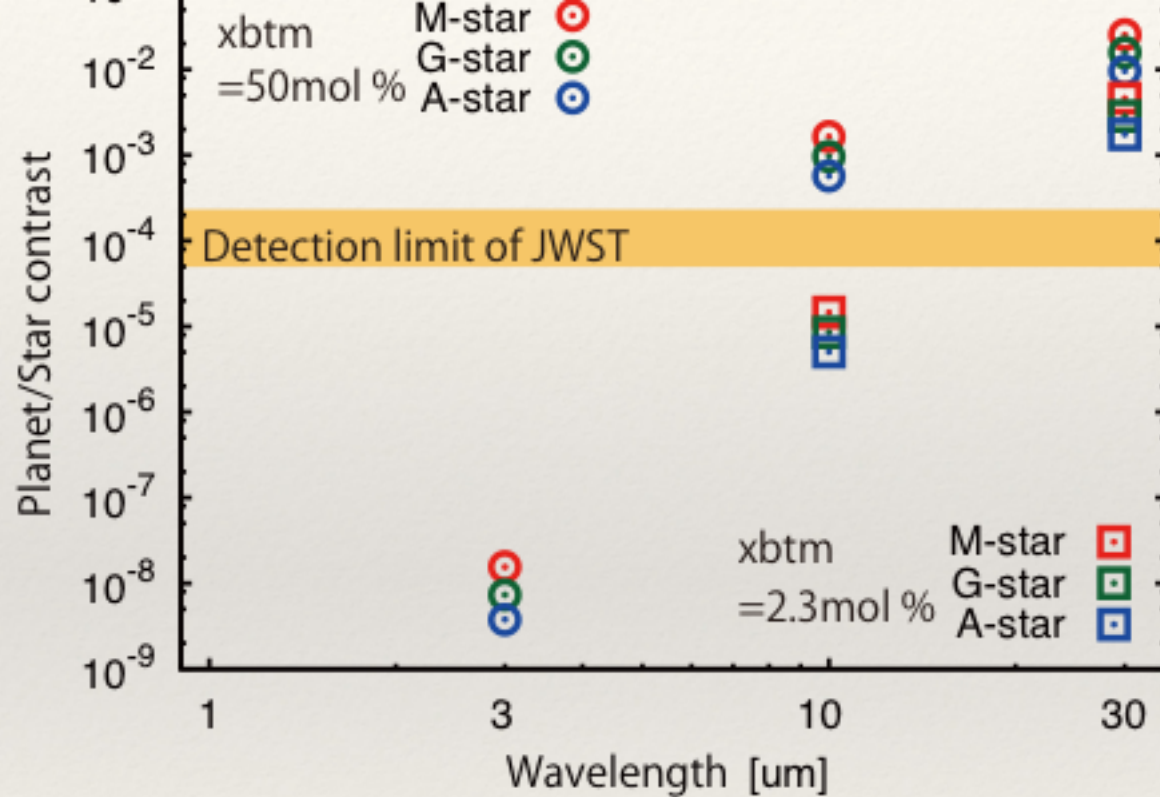
The luminosity become large



In early age, the planet can be easier to detect

Self-luminous Extrasolar Ice giants at Early Age

10⁻¹

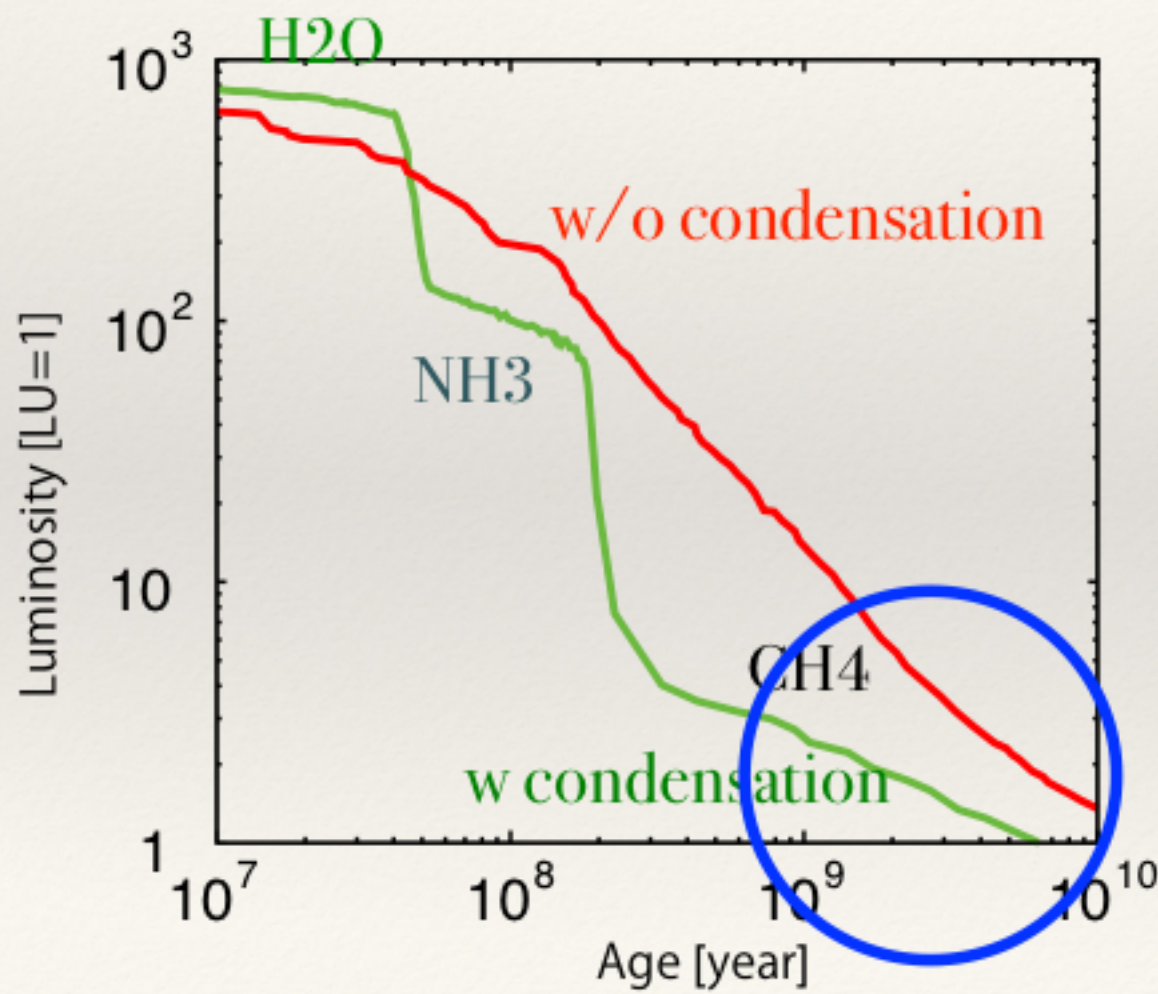


Wavelength longer than 10 μm

→ **Self-luminous ice giant with ice-rich atmosphere can be detected by JWST**

The Effect on the Luminosity at Late Stage

Ice constituents: 65 mol % in the atmosphere



Increase the flux



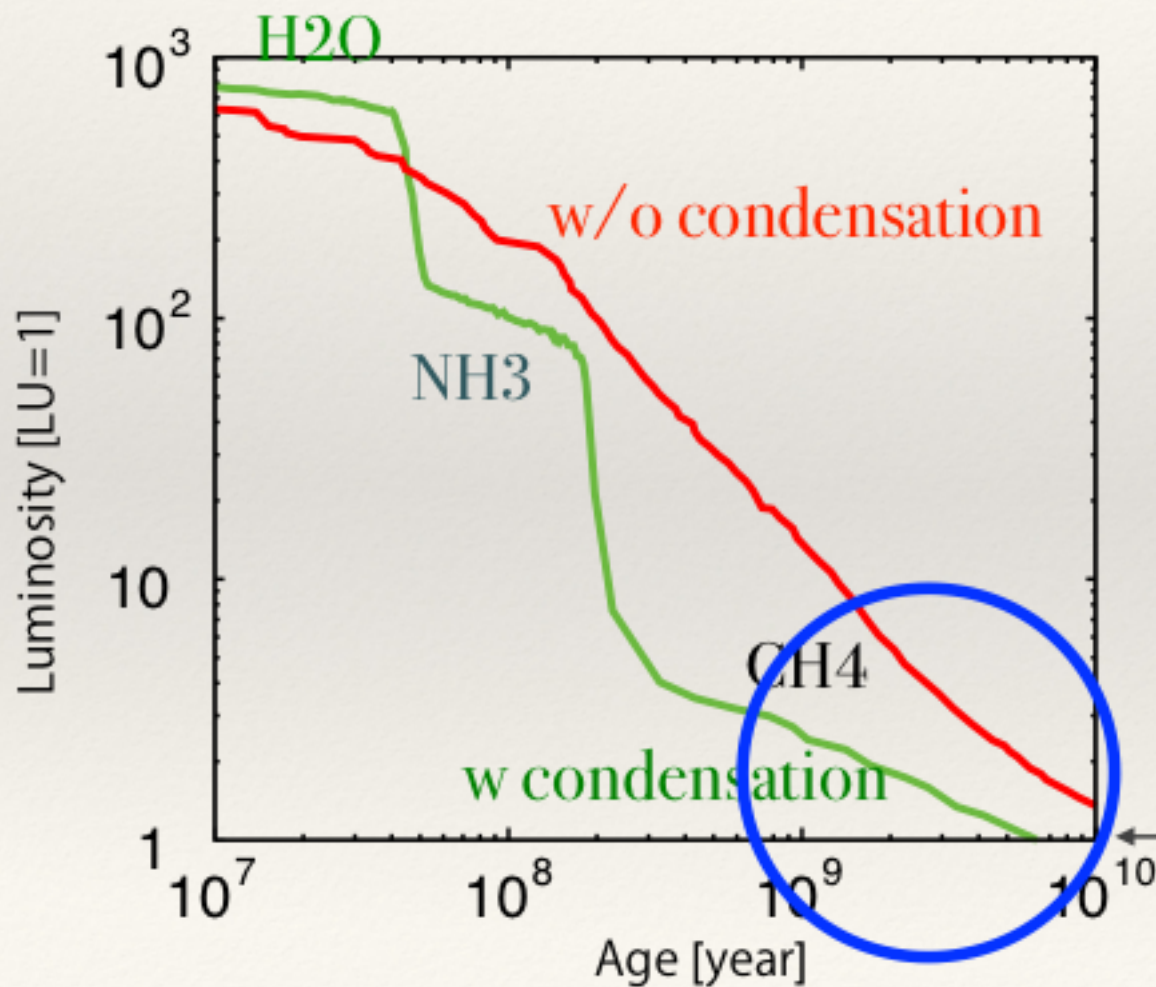
Shorten the evolutionary
timescale of the planet



The planet will cool faster

The Effect on the Luminosity at Late Stage

Ice constituents: 65 mol % in the atmosphere



Increase the flux



Shorten the evolutionary
timescale of the planet



The planet will cool faster

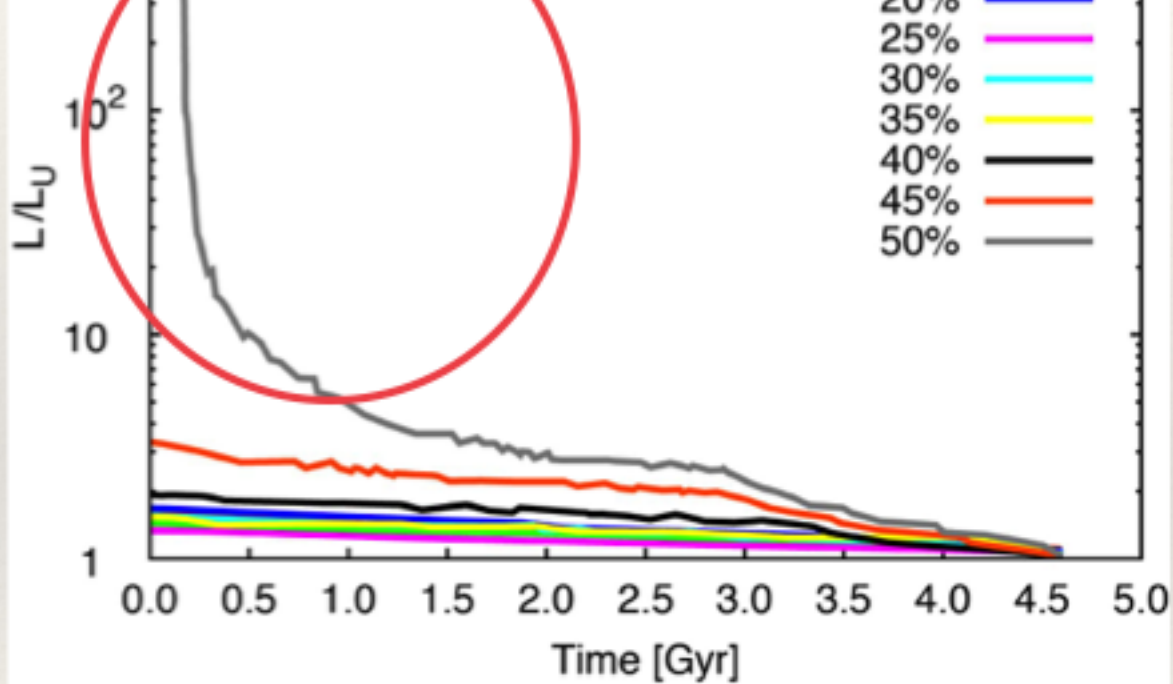
**This effect will important
to explain the Uranian L**

Pearl et al. (1980), Fortney et al. (2011)

Implication for Uranus



The small mol fraction of ice
cannot shorten the timescale



cannot enter into the atmosphere

↓

A significant amount of ice constituents is required

↓

Global event is needed to mix the ice constituents in the atmosphere

Summary

The thermal evolution of the ice giant with the effect of the condensations of water, ammonia, and methane is investigated.

Results

- Condensation of ices causes large outgoing flux.
- The cooling of the ice giant with the condensation is accelerated due to keeping the high temperature in the atmosphere.

Implication For Exoplanets

If the planetary atmosphere is rich in ice constituent at early age, the planetary luminosity is large enough to detect by JWST.

Implication For solar system planets

To explain the present luminosity of Uranus, a significant amount of ice constituents is required immediately after the formation.

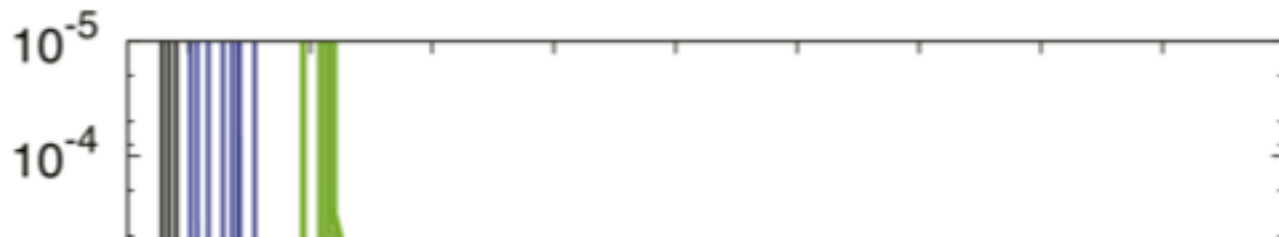
Take Home Message

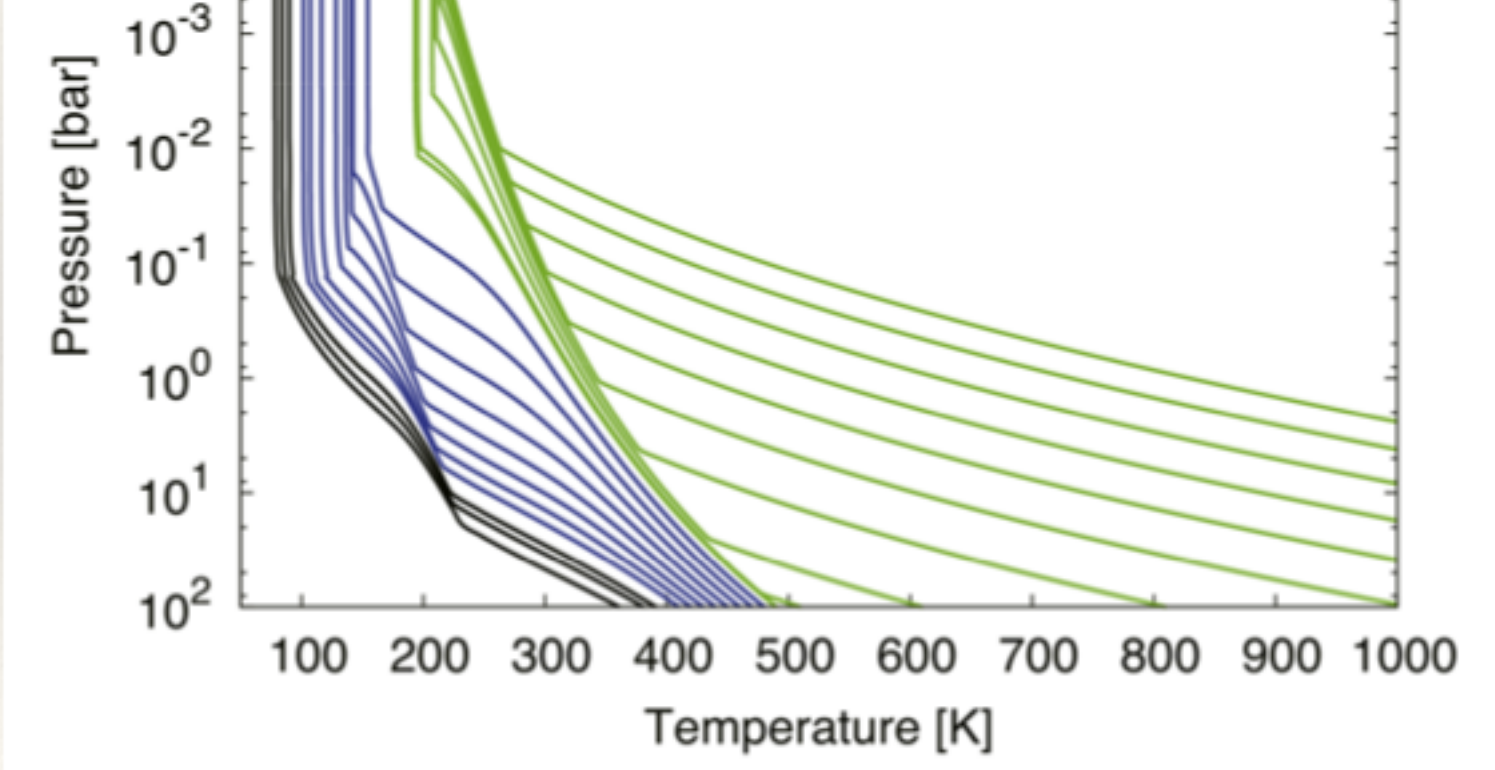
Condensation in atmosphere is very important.

It should change Luminosity & Evolution.

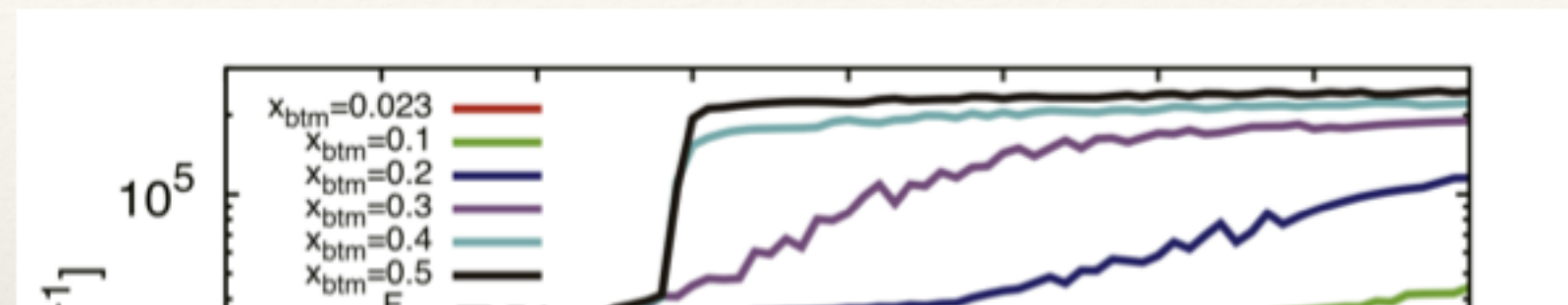
Appendix

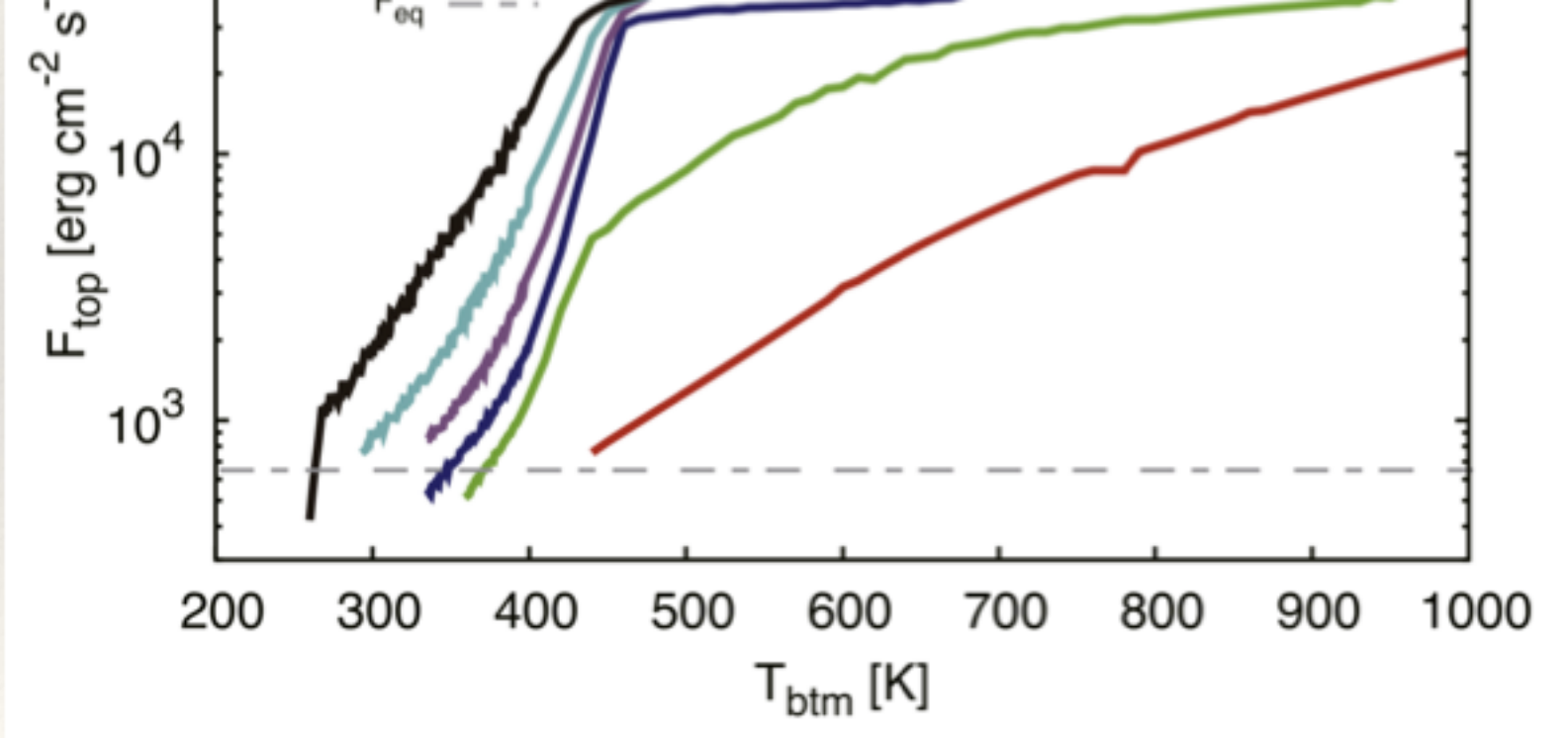
Atmospheric Structure



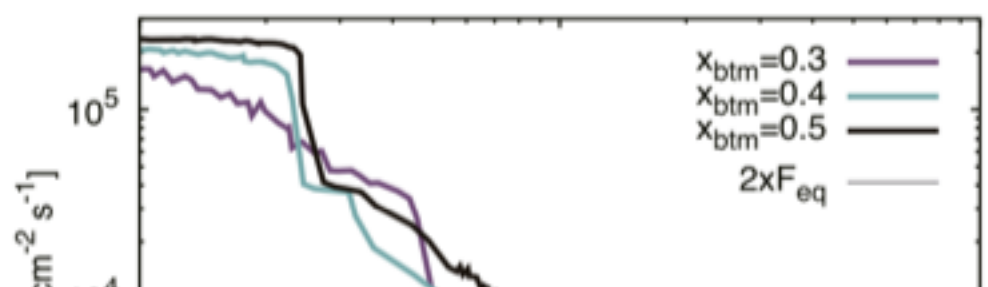
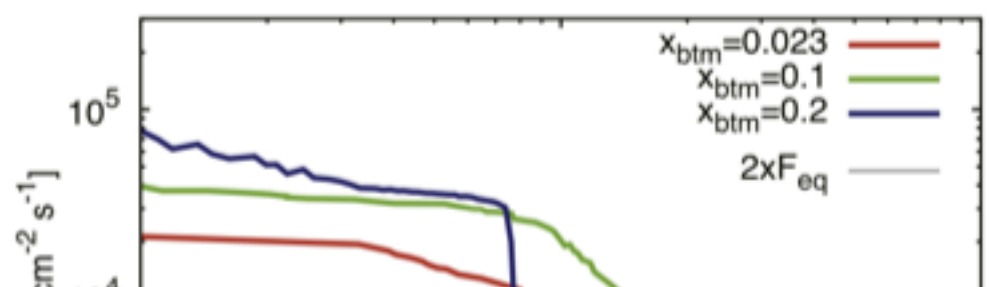


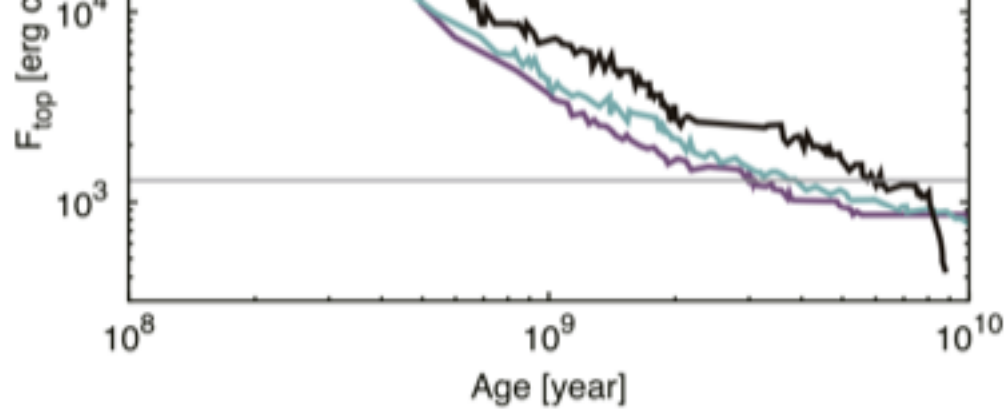
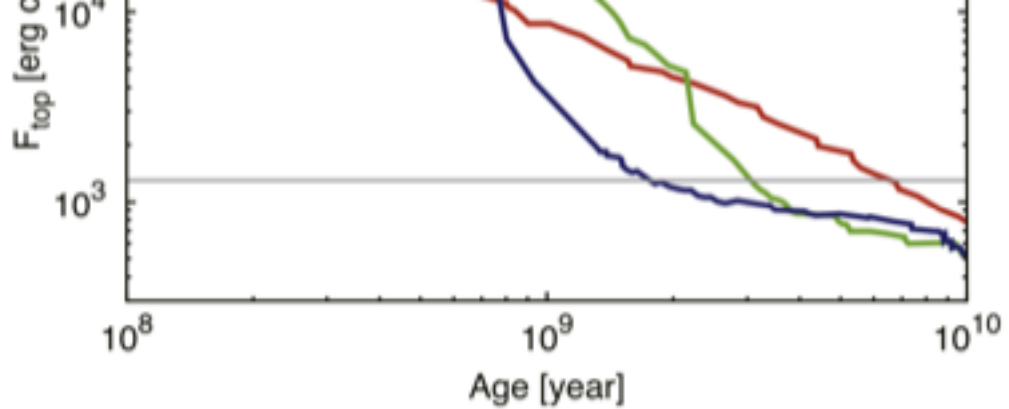
The Outgoing Flux



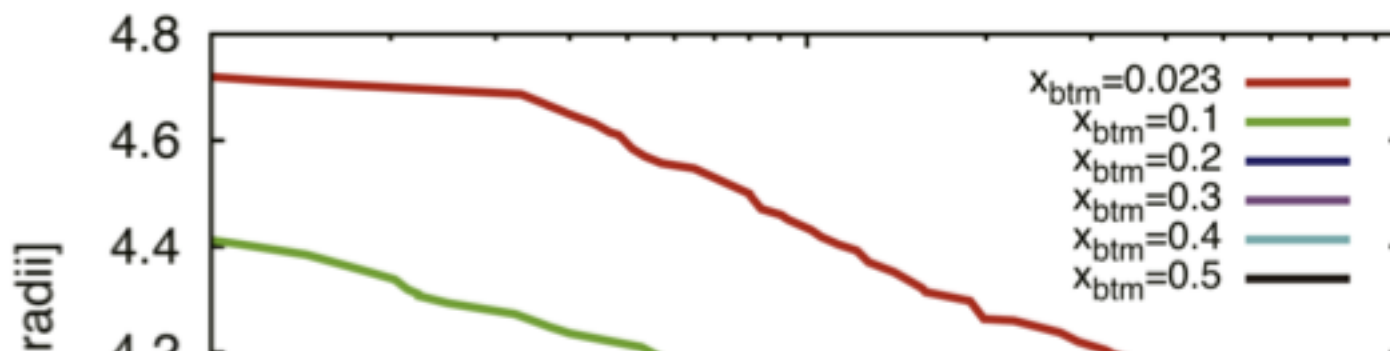


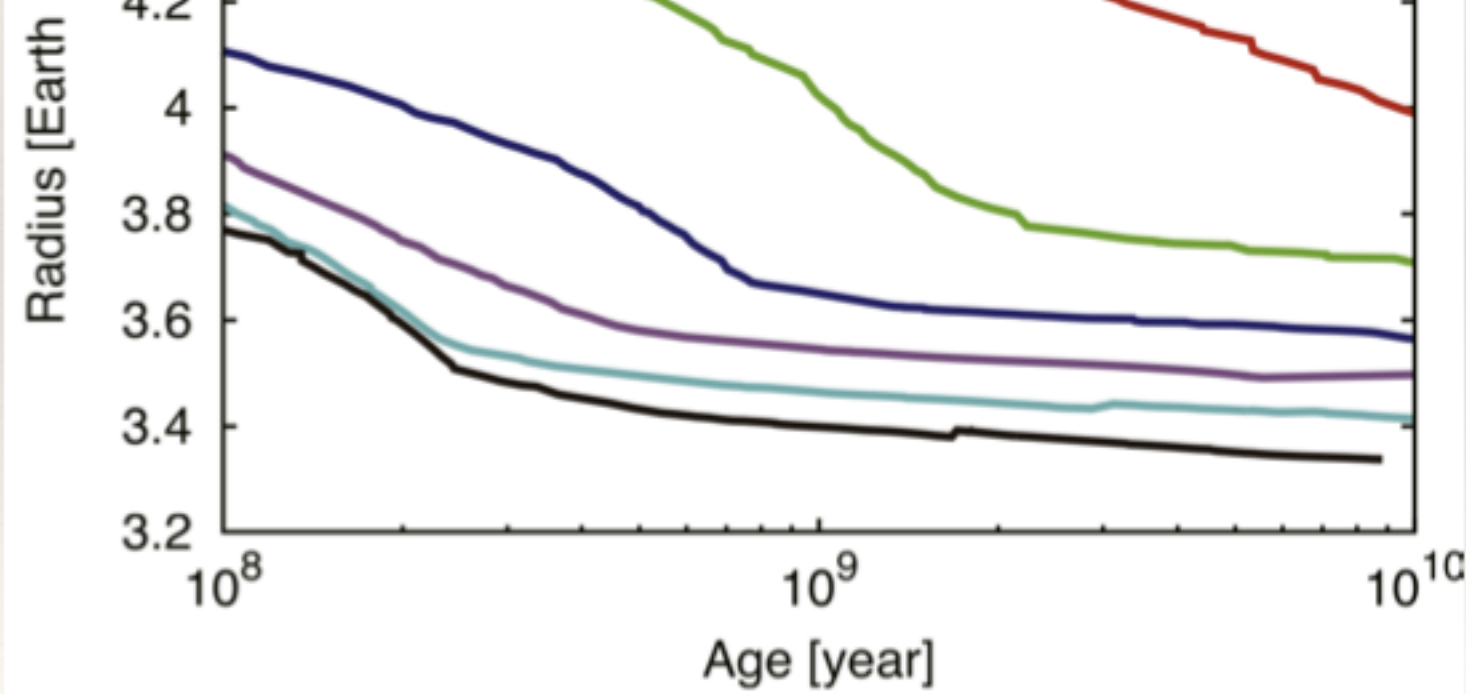
The Effect on Thermal Evolution



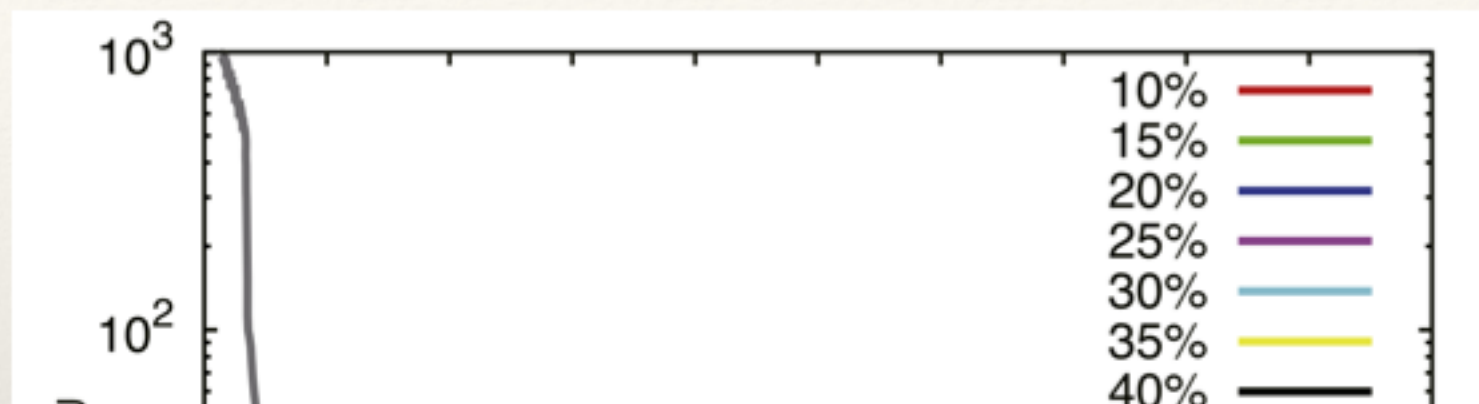


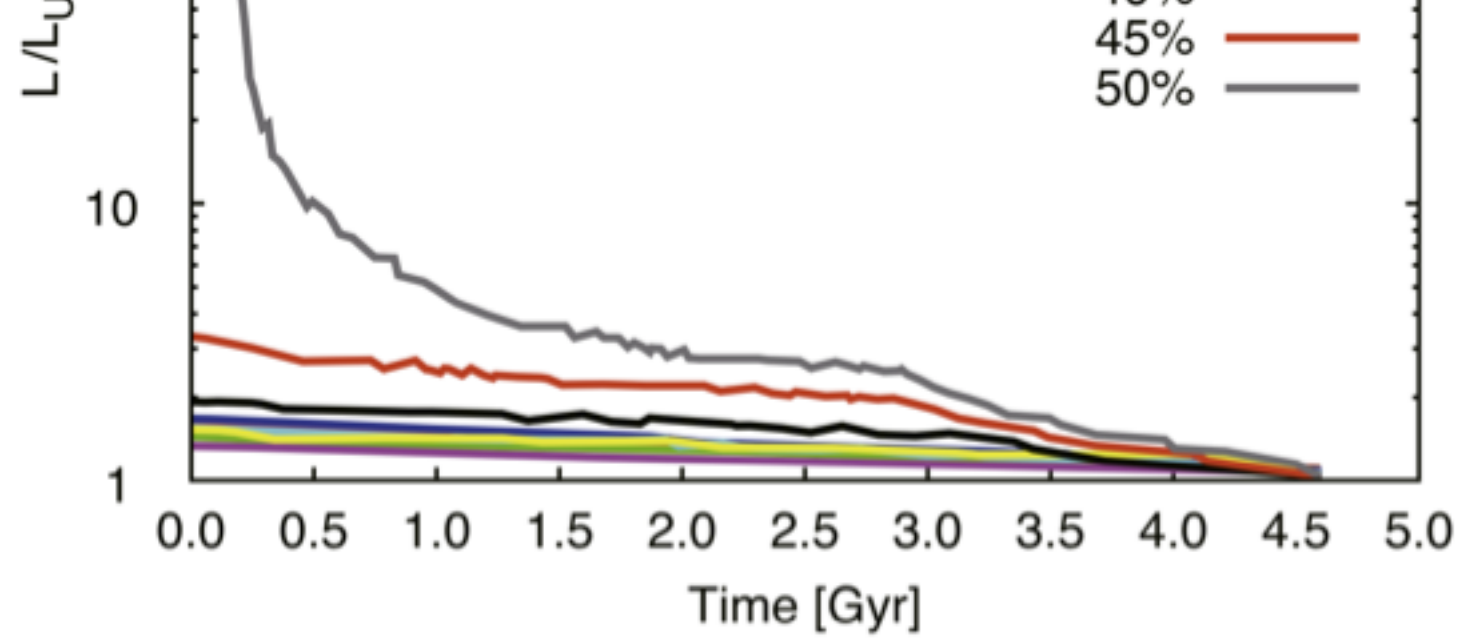
The Effect on Planetary Radius





Implication for Uranus





Methods: Atmospheric structure

Stratosphere

$$\sigma T^4 = F_0 \frac{\tau + 1}{2} + \frac{\sigma T_{\text{eq}}^4}{2} \left[1 + \frac{\kappa_{\text{th}}}{\kappa_{\text{v}}} + \left(\frac{\kappa_{\text{v}}}{\kappa_{\text{th}}} - \frac{\kappa_{\text{th}}}{\kappa_{\text{v}}} \right) e^{-\tau_{\text{v}}} \right] \quad \text{Matsui\&Abe(1986)}$$

F_0 : planetary flux · T : temperature · T_{eq} : equilibrium temperature

Troposphere

No condensation $\longrightarrow \frac{d \ln T}{d \ln P} = \left(\frac{\partial \ln T}{\partial \ln P} \right)_{\text{dry}} = \left(\frac{\partial \ln T}{\partial \ln P} \right)_S$

With condensation $\longrightarrow \frac{d \ln T}{d \ln P} = \left(\frac{\partial \ln T}{\partial \ln P} \right)_S \left[1 + \sum_{i=j+1}^N \frac{x_i}{1-x_i} \frac{d \ln p_i^*}{d \ln T} \right]$

with condensation

$$d \ln P = \left(\frac{\partial \ln P}{\partial \ln T} \right)_{\text{dry}} + \sum_{i=j+1}^N \frac{R_g}{C_p} \frac{x_i}{1-x_i} \frac{d \ln p_i^*}{d \ln T}$$

Condensation curve: $p^*(T)$: NH₃, CH₄ => Sanchez-Lavega et al. (2004), H₂O => Nakajima et al. (1992)

Opacities

Line profiles: calculated by HITRAN2012 (Rothman et al. 2013)

The Rosseland mean opacities is used

$$\frac{1}{\kappa_{\text{th}}} = \int_0^\infty \frac{1}{\kappa_\nu} \frac{dB_\nu(T_{\text{atm}})}{dT} d\nu \bigg/ \int_0^\infty \frac{dB_\nu(T_{\text{atm}})}{dT} d\nu$$

The tropopause is determined by the flux profile

Methods: Interior structure

Hydrostatic equilibrium

$$\frac{\partial P}{\partial M_r} = -\frac{GM_r}{4\pi r^4}$$

$$\frac{\partial r}{\partial M_r} = -\frac{1}{4\pi r^2 \rho}$$

$$\frac{\partial T}{\partial M_r} = -\frac{\partial P}{\partial M_r} \frac{T}{P} \nabla$$

$$\nabla = \nabla_{\text{ad}} = \left(\frac{\partial \ln T}{\partial \ln P} \right)$$

Equations of state

H-He Saumon et al. (1995)

H₂O Lyon et al. (1992), SESAME 7150

Rocky core: MgSiO₃ (Interpolated by Vinet EOS)

Perovskite+Ferromagnesiowstite

→ Stixrude & Lithgow-Bertelloni (2005)

$$v = v_{ad} - \left(\frac{\partial \ln P}{\partial s} \right)_s$$

Post-perovskite+Ferromagnesiowstite

→ Tsuchiya et al. (2004)

The mixture of **H-He+H₂O** is assumed **the volume additive law**

$$\frac{1}{\rho} = (1 - Z_0) \left(\frac{X}{\rho_H} + \frac{Y}{\rho_{He}} \right) + \frac{Z_0}{\rho_{H_2O}}$$

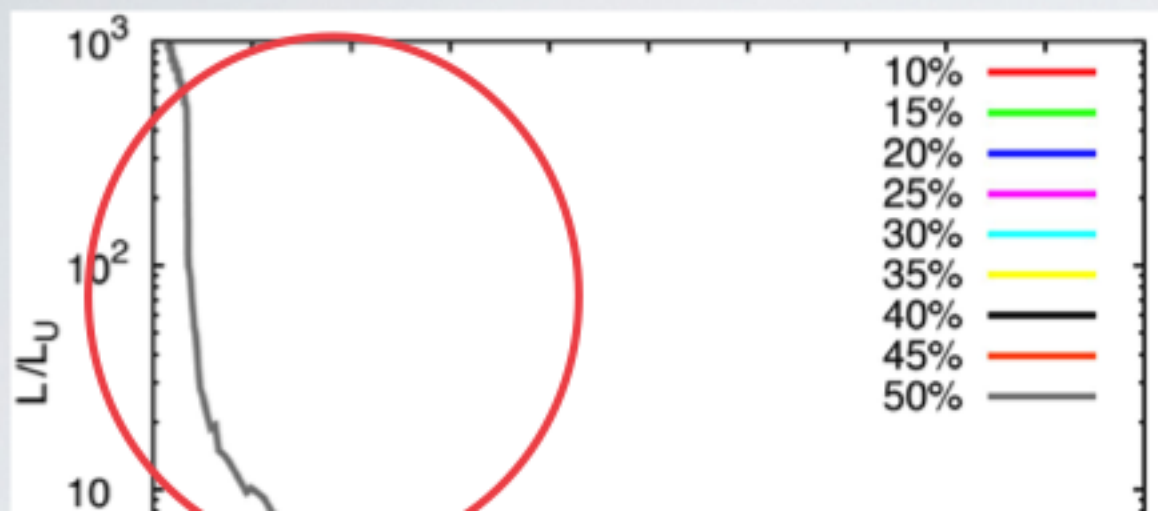
mass fraction for hydrogen and helium, X=0.75, Y=0.25

H₂O mass fraction Z₀=0.3

$$S = XS_H + YS_{He} + Z_0S_{H_2O} + S_{mix} \quad (S_{mix} \Rightarrow \text{mixing entropy for ideal gases})$$

validity: Soubiran&Militzer(2015)

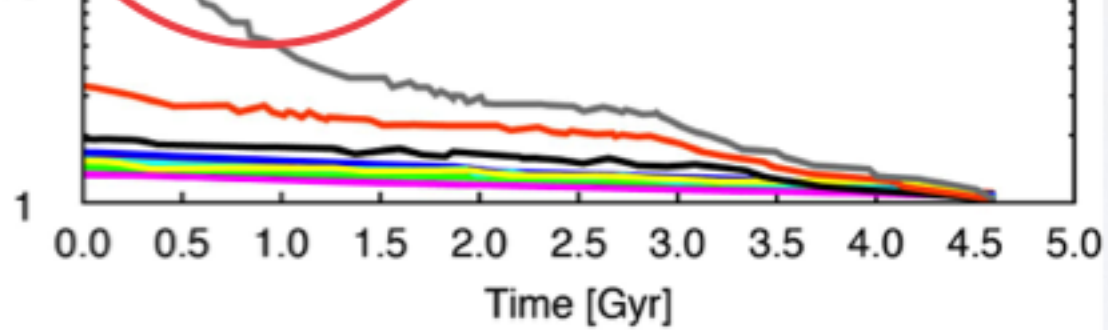
Results 3: The dependence on the initial ice mol fraction



The small mol fraction of ice cannot shorten the timescale



A significant amount of



Ice constituents is required



Global event is needed to mix the ice constituents in the atmosphere